

Direct Adaptive H_∞ Control for a Class of Nonlinear Systems based on LS-SVM

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Abstract: A scheme of direct adaptive H_∞ control based on least squares support vector machines (LS-SVM) is proposed for a class of nonlinear uncertain systems. In this method, LS-SVM is employed to construct the adaptive controller, and an on-line learning rule for the weighting vector and bias is derived. A parameter selection method based on the genetic algorithm (GA) is given for LS-SVM regression with Gauss kernel. H_∞ control is used to attenuate the effect on the tracking error caused by LS-SVM approximation errors and external disturbances. Lyapunov theory is used to prove the uniformly ultimately bounded stability of the close-loop system. The simulation result shows the effectiveness and feasibility of the proposed method.

Keywords: Least Squares Support Vector Machines, Nonlinear Systems, Adaptive Control, H_∞ Control, Genetic Algorithm

1 Introduction

Least squares support vector machines (LS-SVM) has been proposed by Suykens et al. for modeling and control of nonlinear systems [1,2]. LS-SVM takes equality in instead of inequality constrains of SVM in the problem formulation such that LS-SVM is easy to train, which promotes the applications of LS-SVM and many function approximation and nonlinear control problems have been tackled with LS-SVM in the last decades [3,4,5,6]. However, those works lack the definite stability proof of the closed loop system using LS-SVM approaches.

A direct adaptive controller is developed incorporating LS-SVM, Lyapunov theory and H_∞ control theory under plant uncertainties and external disturbances in this paper. In this method, the LS-SVM is employed to approximate unknown nonlinear dynamics in the plant, and then the tracking error caused by LS-SVM approximation errors and external disturbance are tackled as the complex interference. To improve the resulting approximation precise, an innovative optimization algorithm known as the genetic algorithm (GA) [7,8] are adopted to automatically tune two parameters in LS-SVM design. It is shown that the designed controller ensures not only guarantee the asymptotic stability of the

close-loop system, but also guarantees the tracking error to satisfy the set performance index by introducing H_∞ control. The numerical simulation is presented to show the effectiveness of the proposed method.

This paper is organized as follows. Section 2 presents the background about control problem in a class of nonlinear uncertain systems. LS-SVM and its parameters selection are briefly described in Section 3. The proposed direct adaptive H_∞ controller based on LS-SVM is designed in Section 4. Numerical examples are given to illustrate the effectiveness of the proposed method in section 5. Finally, conclusions are offered in Section 6.

2 Problem Formulation

Consider the n th-order nonlinear systems of the form

$$\begin{cases} \dot{x}^{(n)} = f(x, \dot{x}, \dots, x^{(n-1)}) + bu + d \\ y = x \end{cases} \quad (1)$$

where f is unknown but bounded continuous function, b is a positive unknown constant, d is a bounded disturbance signal of the system, $u \in R$ and $y \in R$ are the input and the output of the system, respectively. Let

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$\mathbf{x} = (x, \dot{x}, \dots, x^{(n-1)})^T \in R^n$ is the state vector of the system which is assumed to be available.

Let y_m be a bounded reference signal, and $e = y_m - y$ the output tracking error.

The control objective is to force y follow the given reference signal y_m under the constraints that all signals involved must be bounded. Hence a feedback control $u(\mathbf{x}|\mathbf{W})$ base on LS-SVM and an adaptive law for adjusting the parameter vector \mathbf{W} of LS-SVM are both determined to satisfy the following conditions.

(1) the closed-loop system is globally stable in the sense that all variables involved must be uniformly bounded.

(2) the following H_∞ tracking performance will be achieved with the given inhibitory level $\rho > 0$,

$$\int_0^{\bar{t}} \mathbf{e}^T \mathbf{Q} \mathbf{e} \leq \mathbf{e}^T(0) \mathbf{P} \mathbf{e}(0) + \frac{1}{\eta} \tilde{\mathbf{W}}^T(0) \tilde{\mathbf{W}}(0) + \rho^2 \int_0^{\bar{t}} \omega^T \omega dt \tag{2}$$

Where $\bar{t} \in [0, \infty]$, $\mathbf{e} = [e, \dot{e}, \dots, e^{(n-1)}]^T$, $\omega \in L_2[0, T]$, $\mathbf{Q} = \mathbf{Q}^T \geq 0$ and $\mathbf{P} = \mathbf{P}^T \geq 0$. ω is the compound interference caused by LS-SVM approximation errors and external disturbance, \mathbf{W} is the parameter vector of LS-SVM, $\tilde{\mathbf{W}}$ is the estimate error vector of the LS-SVM, $\eta > 0$ is the learning rate of LS-SVM.

3 LS-SVM and Its Parameter Selection

3.1 LS-SVM Regression

In the section, we briefly discuss LS-SVM regression. For further details on LS-SVM we refer to Ref. [1].

Given the following training sample set(D): $D = \{(\mathbf{x}_k, y_k) | k = 1, 2, \dots, N\}$, where is the total number of training data pairs, $\mathbf{x}_k \in R^n$ is the regression vector and $y_k \in R$ is the output. The following model is taken

$$f(\mathbf{x}) = \mathbf{w}^T \boldsymbol{\varphi}(\mathbf{x}) + b \tag{3}$$

where the nonlinear mapping $\boldsymbol{\varphi} : R^n \rightarrow R^{n_h}$ maps the input data into a so-called high dimensional feature space (which can be infinite dimension). The regularized cost function of the LS-SVM is given as:

$$\min J(\mathbf{w}, \boldsymbol{\varepsilon}) = \frac{1}{2} \mathbf{w}^T \mathbf{w} + \frac{1}{2} \gamma \sum_{k=1}^N \boldsymbol{\varepsilon}_k^2 \tag{4}$$

s.t. $y_k = \mathbf{w}^T \boldsymbol{\varphi}(\mathbf{x}_k) + b + \boldsymbol{\varepsilon}_k, k = 1, 2, \dots, N$

where $\mathbf{w} \in R^{n_h}$ is the weight vector, $\boldsymbol{\varepsilon}_k \in R$ is slack variable, $b \in R$ is a bias term and $\gamma \in R$ is regularization item. The Lagrangian corresponding to Eq. (4) can be defined as follows:

$$L(\mathbf{w}, b, \boldsymbol{\varepsilon}; \boldsymbol{\alpha}) = J(\mathbf{w}, \boldsymbol{\varepsilon}) - \sum_{k=1}^N \alpha_k \{ \mathbf{w}^T \boldsymbol{\varphi}(\mathbf{x}_k) + b + \boldsymbol{\varepsilon}_k - y_k \} \tag{5}$$

where $\alpha_k \in R(k = 1, 2, \dots, N)$ are the Lagrange multipliers. Using the Karush-Kuhn-Tucker (KKT) conditions, we get the linear equations

$$\begin{bmatrix} b \\ \boldsymbol{\alpha} \end{bmatrix} = \begin{bmatrix} 0 & \bar{\mathbf{1}}^T \\ \bar{\mathbf{1}} & \Delta + \gamma^{-1} \mathbf{I} \end{bmatrix}^{-1} \begin{bmatrix} 0 \\ \mathbf{y} \end{bmatrix} \tag{6}$$

with $\mathbf{y} = [y_1, \dots, y_N]^T \in R^N$, $\bar{\mathbf{1}} = [1, \dots, 1]^T \in R^N$, $\boldsymbol{\alpha} = [\alpha_1, \dots, \alpha_N]^T$, $\Delta_{kl} = \boldsymbol{\varphi}(\mathbf{x}_k)^T \boldsymbol{\varphi}(\mathbf{x}_l) = K(\mathbf{x}_k, \mathbf{x}_l), \forall k, l = 1, 2, \dots, N$ is the kernel function satisfying Mercer's condition. In this paper, the Gaussian RBF kernel $K(\mathbf{x}_k, \mathbf{x}_l) = \exp(-\|\mathbf{x}_k - \mathbf{x}_l\|^2 / 2\sigma^2)$ is chosen as the kernel function, where σ is the kernel parameter. And the resulting LS-SVM regression model becomes

$$f(\mathbf{x}) = \sum_{k=1}^N \alpha_k K(\mathbf{x}, \mathbf{x}_k) + b \tag{7}$$

where α_k, b are the solution to Eq. (6).

It is well known that LS-SVM generalization performance depends on a good setting of regularization parameter γ and the kernel parameter σ . In order to achieve the better generalization performance, the parameters of LS-SVM can be selected by GA.

3.2 Hyper-Parameters based on GA Algorithm

For the problem of parameters selection by GA, each set of γ and σ is taken as an individual in a population, and the estimated generalization error as the fitness. As the k -fold cross-validation is a very reliable method to estimate the generalization error [1, 2], it is employed in this paper. In k -fold cross-validation, the training data is randomly split into k roughly equal subsets. An LS-SVM decision rule is trained using $(k - 1)$ of these subsets and validated on the subset left out. This procedure is repeated k times with each of the k subsets used as the validation subset in turn. Averaging the validation errors over the k trials gives an estimate of the generalization error. The flowchart of the GA-based parameters selection algorithm for the LS-SVM is shown in Fig. 1.

4 Direct Adaptive H_∞ Controller Design and Stability Analysis Based on LS-SVM

First, let $\mathbf{k} = (k_n, k_{n-1}, \dots, k_1)^T \in R^n$ be such that all roots of the polynomial $h(s) = s^n + k_1 s + \dots + k_n$ are in the open left-hand plane. If the function f and the constant b are known, and $d = 0$, then the control law

$$u^* = \frac{1}{b} [-f(\mathbf{x}) + y_m^{(n)} + \mathbf{k}^T \mathbf{e}] \tag{8}$$

applied to system (1) can result in $e^{(n)} + k_1 e^{(n-1)} + \dots + k_n e = 0$, which implies that

$\lim_{t \rightarrow \infty} e(t) = 0$ (the main objective of control). Since f and b are unknown, and $d \neq 0$, then the optimal control u^* can not be implemented. Hence, the adaptive controller based on LS-SVM will be designed to approximate this optimal control.

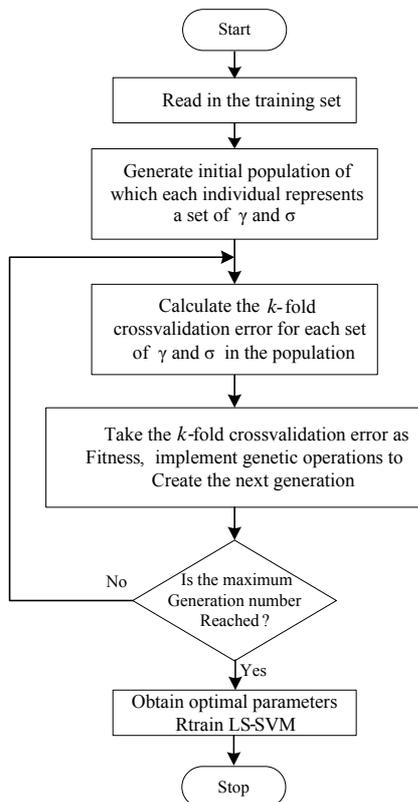


Fig. 1 Structure of least support vector machines

The control u is supposed to consist of an adaptive control $\hat{u}(\mathbf{x}|\mathbf{W})$ based on LS-SVM and a H_∞ robust control v , i.e.,

$$u = \hat{u}(\mathbf{x}|\mathbf{W}) - v \tag{9}$$

where

$$v = -\frac{1}{r} \mathbf{B}^T \mathbf{P} \mathbf{e} \tag{10}$$

$r > 0$ is a design parameter, \mathbf{P} is a symmetric positive definite matrix satisfying the Riccati equation

$$\mathbf{P} \mathbf{A} + \mathbf{A}^T \mathbf{P} + \mathbf{Q} - \frac{2}{r} \mathbf{P} \mathbf{B} \mathbf{B}^T \mathbf{P} + \frac{2}{\rho^2} \mathbf{P} \mathbf{B} \mathbf{B}^T \mathbf{P} = 0 \tag{11}$$

where $r \leq 2\rho^2$. Substituting (9) into (1), we will have

$$\dot{x}^{(n)} = f(\mathbf{x}) + b[\hat{u}(\mathbf{x}|\mathbf{W}) - v] + d \tag{12}$$

After some straightforward manipulation, we can obtain the error of the closed-loop system

$$\dot{\mathbf{e}} = \mathbf{A} \mathbf{e} + \mathbf{B}[u^*(\mathbf{x}) - \hat{u}(\mathbf{x}|\mathbf{W})] + \mathbf{B}v - \mathbf{B}d/b \tag{13}$$

where

$$\mathbf{A} = \begin{bmatrix} 0 & 1 & 0 & \cdots & 0 & 0 \\ 0 & 0 & 1 & \cdots & 0 & 0 \\ \cdots & \cdots & \cdots & \cdots & \cdots & \cdots \\ 0 & 0 & 0 & \cdots & 0 & 1 \\ -k_n & -k_{n-1} & -k_{n-2} & \cdots & -k_2 & -k_1 \end{bmatrix}, \mathbf{B} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ b \end{bmatrix}$$

LS-SVM is used to approximate the optimal control. The output of LS-SVM is

$$\hat{u}(\mathbf{x}|\mathbf{W}) = \mathbf{W}^T \boldsymbol{\beta} \tag{14}$$

where

$$\mathbf{W} = [w_1 \ w_2 \ \cdots \ w_{N+1}]^T, \boldsymbol{\beta}(\mathbf{x}) = [1, K(\mathbf{x}_1, \mathbf{x}), \cdots, K(\mathbf{x}_N, \mathbf{x})]^T.$$

The following objective is to design the control u and the adaptive law of the weight vector \mathbf{W} to realize the control task. First, the optimal weight vector \mathbf{W}^* is defined as

$$\mathbf{W}^* = \arg \min_{\mathbf{W} \in \Omega} \left[\sup_{\mathbf{x} \in D} |\hat{u}(\mathbf{x}|\mathbf{W}) - u^*(\mathbf{x})| \right] \tag{15}$$

where $\Omega = \{\mathbf{W} | \|\mathbf{W}\| \leq M\}$ and $D = \{\mathbf{x} | \|\mathbf{x}\| \leq M_1\}$ are the feasible region of the weight vector and the state vector, respectively, M and M_1 are specified by the designer. We assume that \mathbf{W} and \mathbf{x} never reach the boundary Ω and D . The minimum approximation error is defined as

$$\omega_n = u^*(\mathbf{x}) - \hat{u}(\mathbf{x}|\mathbf{W}^*) \tag{16}$$

Substituting (14) and (16) into (13), we get the error equation of the closed-loop system

$$\dot{\mathbf{e}} = \mathbf{A} \mathbf{e} + \mathbf{B}\{[u^*(\mathbf{x}) - \hat{u}(\mathbf{x}|\mathbf{W}^*)] + [\hat{u}(\mathbf{x}|\mathbf{W}^*) - \hat{u}(\mathbf{x}|\mathbf{W})]\} + \mathbf{B}v - \mathbf{B}d/b \tag{17}$$

or equivalently

$$\dot{\mathbf{e}} = \mathbf{A} \mathbf{e} - \mathbf{B} \tilde{\mathbf{W}}^T \boldsymbol{\beta} + \mathbf{B}v + \mathbf{B}\omega \tag{18}$$

where $\omega = \omega_n - d/b$, and $\tilde{\mathbf{W}} = \mathbf{W} - \mathbf{W}^*$ is the estimate error of the parameter vector \mathbf{W} .

$$\dot{\tilde{\mathbf{W}}} = \eta \mathbf{e}^T \mathbf{P} \mathbf{B} \boldsymbol{\beta} \tag{19}$$

Theorem. For the nonlinear system (1) if the adaptive control scheme based on LS-SVM is chosen as (9), and the adaptive law of the parameter is chosen as (19), then the whole adaptive control scheme guarantees the following properties:

- i) $\mathbf{x}, u \in L_\infty$.
- ii) the following H_∞ tracking performance (2) will be achieved with the given inhibitory level ρ .

Proof. We choose the Lyapunov function as

$$V = \frac{1}{2} \mathbf{e}^T \mathbf{P} \mathbf{e} + \frac{1}{2\eta} \tilde{\mathbf{W}}^T \tilde{\mathbf{W}} \tag{20}$$

Differentiated with respect to t , we get

$$\dot{V} = \frac{1}{2}(\dot{\mathbf{e}}^T \mathbf{P} \mathbf{e} + \mathbf{e}^T \dot{\mathbf{P}} \mathbf{e}) + \frac{1}{2\eta}(\dot{\tilde{\mathbf{W}}}^T \tilde{\mathbf{W}} + \tilde{\mathbf{W}}^T \dot{\tilde{\mathbf{W}}}) \quad (21)$$

Since $\dot{\tilde{\mathbf{W}}} = \dot{\mathbf{W}}$, and according to (18), (21) becomes

$$\begin{aligned} \dot{V} = & \frac{1}{2}[\mathbf{e}^T \mathbf{A}^T \mathbf{P} \mathbf{e} + \nu \mathbf{B}^T \mathbf{P} \mathbf{e} - \tilde{\mathbf{W}}^T \beta \mathbf{B}^T \mathbf{P} \mathbf{e} + \\ & \omega \mathbf{B}^T \mathbf{P} \mathbf{e} + \frac{1}{\eta} \tilde{\mathbf{W}}^T \dot{\tilde{\mathbf{W}}} + \mathbf{e}^T \mathbf{P} \mathbf{A} \mathbf{e} + \mathbf{e}^T \mathbf{P} \mathbf{B} \nu - \\ & \mathbf{e}^T \mathbf{P} \mathbf{B} \tilde{\mathbf{W}}^T \beta + \mathbf{e}^T \mathbf{P} \mathbf{B} \omega + \frac{1}{\eta} \tilde{\mathbf{W}}^T \dot{\tilde{\mathbf{W}}}] \end{aligned} \quad (22)$$

From (10), we can obtain

$$\dot{V} = \frac{1}{2}[\mathbf{e}^T (\mathbf{P} \mathbf{A} + \mathbf{A}^T \mathbf{P} - \frac{2}{\rho} \mathbf{e}^T \mathbf{P} \mathbf{B} \mathbf{B}^T \mathbf{P}) \mathbf{e} - \tilde{\mathbf{W}}^T (\beta \mathbf{B}^T \mathbf{P} \mathbf{e} - \frac{1}{\eta} \dot{\tilde{\mathbf{W}}}) + \frac{1}{2} \omega \mathbf{B}^T \mathbf{P} \mathbf{e} + \frac{1}{2} \mathbf{e}^T \mathbf{P} \mathbf{B} \omega] \quad (23)$$

Based on the adaptive law (19) and the Riccati equation (11), we can obtain

$$\begin{aligned} \dot{V} = & -\frac{1}{2} \mathbf{e}^T \mathbf{Q} \mathbf{e} - \frac{1}{2\rho^2} \mathbf{e}^T \mathbf{P} \mathbf{B} \mathbf{B}^T \mathbf{P} \mathbf{e} + \frac{1}{2} \omega \mathbf{B}^T \mathbf{P} \mathbf{e} \\ = & -\frac{1}{2} \mathbf{e}^T \mathbf{Q} \mathbf{e} - \frac{1}{2} \left(\frac{1}{\rho} \mathbf{B}^T \mathbf{P} \mathbf{e} - \rho \omega \right)^T \left(\frac{1}{\rho} \mathbf{B}^T \mathbf{P} \mathbf{e} - \rho \omega \right) + \frac{1}{2} \rho^2 \omega^2 \\ \leq & -\frac{1}{2} \mathbf{e}^T \mathbf{Q} \mathbf{e} + \frac{1}{2} \rho^2 \omega^2 \leq -\frac{1}{2} \lambda_{\min}(\mathbf{Q}) \|\mathbf{e}\|^2 + \frac{1}{2} \rho^2 |\bar{\omega}|^2 \end{aligned} \quad (24)$$

where $\bar{\omega}$ is the upper bound of ω , $\lambda_{\min}(\mathbf{Q})$ is the minimum eigenvalue of the matrix \mathbf{Q} . From the above equation, we can know when $\|\mathbf{e}\| \geq \rho |\bar{\omega}| / \lambda_{\min}(\mathbf{Q})$, then $\dot{V} < 0$. Hence, we can establish that $\mathbf{x}, u \in L_\infty$.

Integrating the above equation from 0 to \bar{t} yields

$$V(\bar{t}) - V(0) \leq -\frac{1}{2} \int_0^{\bar{t}} \mathbf{e}^T \mathbf{Q} \mathbf{e} dt + \frac{1}{2} \rho^2 \int_0^{\bar{t}} \omega^T \omega dt \quad (25)$$

Since $V(\bar{t}) \geq 0$, from (25) we can obtain

$$\begin{aligned} \frac{1}{2} \int_0^{\bar{t}} \mathbf{e}^T \mathbf{Q} \mathbf{e} dt \leq & V(0) + \frac{1}{2} \rho^2 \int_0^{\bar{t}} \omega^2 dt = \frac{1}{2} \mathbf{e}^T(0) \mathbf{P} \mathbf{e}(0) + \\ & \frac{1}{2\eta} \tilde{\mathbf{W}}^T(0) \tilde{\mathbf{W}}(0) + \frac{1}{2} \rho^2 \int_0^{\bar{t}} \omega^T \omega dt \end{aligned} \quad (26)$$

Therefore, the theorem holds. \square

5 Simulation Result

Consider the following nonlinear system

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = -0.1x_2 - x_1^3 + 12 \cos t + u + d \\ y = x_1 \end{cases} \quad (27)$$

where $f = -0.1x_2 - x_1^3 + 12 \cos t$, $b = 1$, d is the square wave disturbance whose vibration amplitude is ± 1 , and period is 2π .

In this example, in order to research the control effect for nonlinear systems, we will adopt the LS-SVM and neural networks to construct the adaptive controller, respectively. The reference signal is assumed to be $y_m = \sin t$. Let $\mathbf{k} = [k_2, k_1]^T = [1, 2]^T$, and the control is chosen as

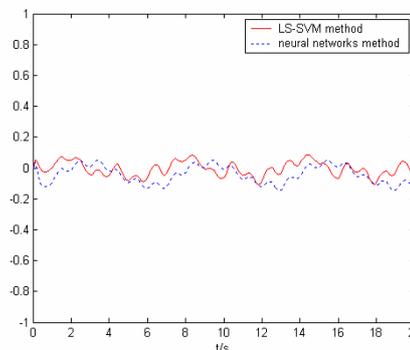
$$u^* = [-0.1x_2 - x_1^3 + 12 \cos t - \sin t + 2\dot{e} + e]$$

The initial condition is assumed to be $x_1(0) = x_2(0) = 0$. To collect the training data, the Gaussian noise with zero mean and standard deviation 1 is selected as the input. By solving the physical model (27) using the fourth-order Runge-Kutta method, the input and output data of (27) are collected. The two-dimensional search space of γ and σ^2 is $[1, 10^4]$ and $[0.1, 10^3]$. The population size and the maximum generation number are set to 30 and 100, respectively. By the proposed GA-based tuning method with the 5-fold cross-validation error as fitness, the optimal set of (γ, σ^2) is found at (5188.8, 9.7).

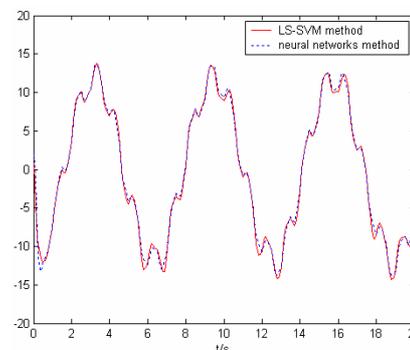
Select the positive definite matrix $\mathbf{Q} = \text{diag}(10, 10)$, and the given inhibitory level $\rho = 0.1, 0.05$, and $r = 0.02, 0.005$. Then after solving the Riccati equation (11), we obtain the positive definite matrix

$$\mathbf{A} = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix}, \mathbf{P} = \begin{bmatrix} 15 & 5 \\ 5 & 5 \end{bmatrix}$$

The simulation results are shown in Fig.2 ($\rho = 0.1$) and Fig.3 ($\rho = 0.05$).

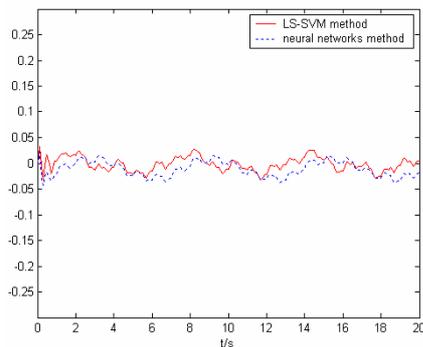


(a) Tracking error

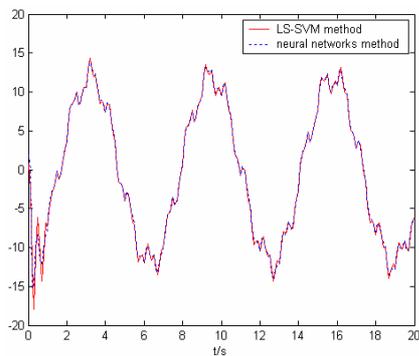


(b) Control input

Fig. 2 Simulation results with $\rho = 0.1$



(a) Tracking error



(b) Control input

Fig. 3 Simulation results with $\rho = 0.05$

According to the simulation results, we can conclude when the value of ρ is smaller, the tracking effect is better, but the control gain is bigger accordingly (the control input ranges from -14.3508 to 13.707 in $\rho = 0.1$, and the control input ranges from -17.8989 to 14.2823 in $\rho = 0.05$). Hence, the reasonable selection for the inhibitory level ρ is very necessary in practical applications.

At the same time, the control precision based on LS-SVM (the average error is 0.0057 with $\rho = 0.1$ and 0.0021 with $\rho = 0.05$) is higher than that based on neural networks (the average error is with $\rho = 0.1$ and 0.0113 with $\rho = 0.05$).

6 Conclusions

A direct adaptive H_∞ control scheme based on LS-SVM is developed for a class of nonlinear uncertain systems. LS-SVM is employed to approximate the optimal control, and an on-line learning rule for the weighting vector and bias is derived. The GA is adopted to optimize the parameters of LS-SVM. H_∞ control is used to attenuate the effect on the tracking error caused by LS-SVM approximation errors and external disturbance. Based on Lyapunov stability theory, it is rigorously proved that the stability of the whole closed-loop system is assured and the tracking performance is achieved.

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