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# A Confidential Communication-Oriented Information Hiding Algorithm based on GHM multi-wavelet and DCT

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Abstract: Structure and energy properties of carrier are considered as the most important factors to information hiding performance. This paper develops a new method to analyze energy and structure characteristics of digital images in order to preprocess the carriers. We adopt GHM multi-wavelet transformation to decompose the cover image into sub-images with different energy level. Then we obtain the embedding regions which are expressed as numerical range by discrete cosine transform. We embed data with different robustness in different regions. Then we get the stego image which is rarely changed in energy and structure properties compared with the original cover image. Experimental results indicate that the invisibility and robustness can be increased separately by 26.87% and 19.25% averagely, and the ability against steganalysis such as RS and Higher Order Statistics based on wavelet coefficients can be improved. Moreover, our algorithm has excellent sensitivity of image processing.

Keywords: Information hiding, GHM multi-wavelet transform, discrete cosine transform, carrier preprocessing, genetic algorithm.

## **1** Introduction

Information hiding is an important approach to secure confidential information transformation. A good information hiding scheme should have reliable performance, such as invisibility, robustness, sensitivity and anti-steganalysis. And performance improvement of information hiding scheme is the most favorite research topic. Currently, most of the schemes have not achieved the above performances at the same time. Schemes based on space domain are good at invisibility, but can not satisfy robustness and anti-steganalysis at the same time [1-3]. The schemes based on transform domain are good at robustness, however, most algorithms are poor in anti-steganalysis [4-6]. According to our previous studies [7], we know that operand-based methods, whether they are space domain- or transform domain-based, don't consider the energy and structure properties of carriers. Although the property analyze of carriers determines the performance of information hiding algorithms.

This paper proposes a preprocessing method based on GHM multi-wavelet transforms and discrete cosine

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transform (DCT) to analyze the energy and structure properties of digital image carriers. Taking advantage of the GHM in energy analyze and DCT in structure analyze, we embed secret information with minimal change in energy and structure of carriers. In particular, GHM multi-wavelet transform can process multi-transformation at the same time, and satisfy compact support and symmetry of the image processing.

#### 2 Information hiding algorithm design

Embedding region: In the digital image processing based on the multi-wavelet transform, the energy distribution due to the order of decomposition and the direction of components. The energy distribution of GHM transform [8] provides a flexible information hiding strategy. Figure 1 shows GHM transform to Lena image. Energy ratio of four First-order GHM Multi-wavelet Transform sub-images is approximately as Table 1 [9].

After GHM multi-wavelet transforms, the most energy not only concentrated in the first-order sub-image  $(LL_1)$ , and also energy distribution of four components is

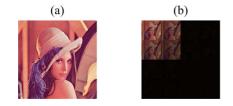


Fig. 1 First-order GHM multi-wavelet transform.

 Table 1
 Energy distribution of first-order GHM multi-wavelet

first-order image	$LL_2$	$LH_2$	$HL_2$	$HH_2$
97.31%	44.76%	21,80%	22.24%	11.20%

Robust Information <u>LL2</u>	Embed Information <u>LH2</u>
Embed Information <u>HL2</u>	Fragile Sign <u>HH2</u>

Fig. 2 Embedded region strategy.

similar to 4.5:2.2:2.2:1.1. Based on the energy distribution of GHM, generation of GHM-DCT embedding region can be divided into four steps:

Step1. Transform the cover image with first-order GHM multi-wavelet to obtain four sub-images such as  $LL_2$ ,  $LH_2$ ,  $HL_2$  and  $HH_2$ . Embed robust parameters in  $LL_2$ . And embed secret information in  $LH_2$  and  $HL_2$ , fragile sign in  $HH_2$ , as shown in Figure 2.

Step2.  $LL_2$  component  $(N \times N)$  will be carried on DCT. Choose the interval distribution  $[(N^2/4)-1, N^2-1]$  of DCT coefficient as embedding region in  $LL_2$ .

Step3.  $LH_2$  and  $HL_2$  ( $N \times N$ ) will also be carried on DCT. Choose the interval distribution  $[0, (N^2/2) - 1]$  of DCT coefficient as embedding region in  $LH_2$  and  $HL_2$ .

Step4. Decomposed  $HH_2$  into  $l\alpha\beta$  color component and transform the  $\beta$  component into gray image. Bit plane decompose to the gray image. The Bit Plane 0 is the embedding region in  $HH_2$ .

Generation of GHM-DCT embedding rules can be divided into four steps:

Rule1. Even and odd coefficients of DCT separately represent as 0 and 1.

Rule2. Embed information into  $LH_2$  and  $HL_2$  with RAID4 (Eight bits is the basic data unit of RAID4).

Rule3. Embed information into  $LL_2$  following a sequential order  $[(N^2/4) - 1, N^2 - 1]$ , and embed information into  $LH_2$  and  $HL_2$  following a sequential order  $[0, (N^2/2) - 1]$ .

Rule4. Embed information into  $HH_2$  by line traversal order.

Information hiding scheme based on GHM Multi-wavelet and DCT can be divided into seven steps:

Step1. Transform the cover image with first-order GHM multi-wavelet to obtain four  $LL_1$  sub-images.

Step2. Transform the  $LH_2$  and  $HL_2$  component  $(N \times N)$  with DCT. Draw the data from DCT coefficient of  $LH_2$  and  $HL_2$  order by  $[0, (N^2/2) - 1]$  according to Rule2. The data separately denoted as  $CLL_1^{(2)}$  and  $CLL_1^{(3)}$ .  $CLL_1^{(2)} = x_1^{(2)}, x_2^{(2)}, \cdots, x_m^{(2)}$  and  $0 \le m \le N^2/2$  . $CLL_1^{(3)} = x_1^{(3)}, x_2^{(3)}, \cdots, x_n^{(3)}$  and  $0 \le n \le N^2/2$ . The final analysis result denoted as C:

$$C = (x_1, x_2, \cdots, x_i) = \left(x_1^{(2)}, x_2^{(2)}, \cdots, x_m^{(2)}, x_1^{(3)}, x_2^{(3)}, \cdots, x_n^{(3)}\right)$$
(1)

Step3. Use Chebyshev map [10] of chaotic map algorithm to optimize information, as defined in Equation (2). Suppose the parameter is  $\mu$ ,  $\eta$  and  $x_k$ . The chaotic sequence after the Chebyshev mapping is  $C_h$ . The Pre-hiding bit series is  $C_p re$ . Scrambling formula is defined in Equation (3), in which  $C_{IN}^x = (b_1^x, b_2^x, \dots, b_{m+n-1}^x, b_{m+n}^x)$ .

$$\begin{cases} 1 , -1 \le x_{k+1} < \eta \\ 0 , \eta \le x_{k+1} \le 1 \end{cases}, x_{k+1} = \cos\left(\mu \arccos(x_k)\right) \quad (2)$$

$$C_{IN}^x = C_{pre} \oplus C_h \tag{3}$$

Step4. In order to optimize the sequence of embedded bits with genetics algorithm [11], suppose F as the amount of the same bit value in matched positions between  $C_{IN}^x$  and C. The optimization model based on GHM-DCT is Equation (4). Get the optimal solution  $x'_n$ ,  $\eta'$  and  $\mu'$  by genetic algorithms optimization.

Step5. Bring  $x'_n$ ,  $\eta'$  and  $\mu'$  into Equation (2) and (3) to get optimization embedded bits  $C^y_{IN} = b^y_1, b^y_2, \dots b^y_{n-1}, b^y_n$ . Embed  $C^x_{IN}$  into DCT coefficients of  $LH_2$  and  $HL_2$  between 0 and  $(N^2/2) - 1$ 

Step6. Transform the  $LL_2$  component  $(N \times N)$  with DCT.  $LL_2$  is the most robust region in four  $LL_1$  sub-images. In order to judge and recover the imperfect information, The CL-DCT embed the check code of RAID4, optimized code of Chebyshev scrambling  $(x'_n, \eta'$  and  $\mu')$  and Hash value of embedding information (recorded as  $R^L$ ) into DCT coefficient between  $(N^2/4) - 1$  and  $N^2 - 1$ .

Step7.  $HH_2$  is the most vulnerable region in four sub-images. Embed the Hash of embedding information (recorded as  $R^H$ ). Receiver can judge whether the stego image is attacked by comparing  $R^H$  and  $R^L$ .

Extracting information:Extracting information is divided into four steps:

Step1. Transform the cover image with first-order GHM multi-wavelet and get four  $LL_1$  sub-images.

Step2. Transform  $LL_2$ ,  $LH_2$  and  $HL_2$  component with DCT. Draw the  $R^L$  from  $LL_2$  component. Draw the

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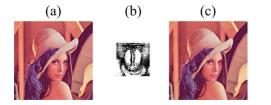


Fig. 3 Hiding and result of GHM-DCT.

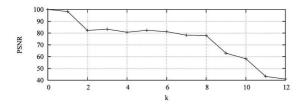


Fig. 4 Experiment of embedding dense and corresponding Invisibility.

data from  $LH_2$  and  $HL_2$  component, and denoted as C''. Draw the  $R^H$  from  $HH_2$ .

Step3. if  $R^L = R^H$ . The C'' is the secret information. if  $R^L \neq R^H$ . The process continues.

Step4. Draw the check code of RAID4 from  $LL_2$  component and use them to process C'' and get final secret information.

#### **3** Simulation experiment

Simulation environment of the algorithm is Matlab7.0.0.19920. Cover image is Lena  $(256 \times 256)$  as shown in Figure.3 (a). Stego image is binary image Baboon  $(64 \times 64)$  as shown in Figure.3 (b).

Invisibility Experiment. Fig.3(c) shows stego image based on GHM-DCT. PSNR value equals 36.8921. It shows that this method is of better invisibility.

Invisibility is determined by Information content. Embed information in 400 images randomly.  $2^k$  is used to denote bit quantity ( $0 \le 2^k \le 4096$ ). Fig. 4 shows the PSNR of different embedding quantity. The experimental results indicated that when  $k \le 12$ , it is of better invisibility ( $PSNR \ge 40.325$ ).

Robustness Experiment. Define texture evaluation and modification rate of binary image  $(N \times N \text{ pixels})$  separately in Equation (4) and (5).

$$w = \frac{\sum_{i=0}^{n-1} \sum_{j=0}^{n-1} f(i,j) \oplus f(i+\mu, j \pm \eta)}{2n^2}$$
(4)

$$p = \frac{\sum_{i=0}^{n-1} \sum_{j=0}^{n-1} f(i,j) \oplus f'(i,j)}{n^2}$$
(5)

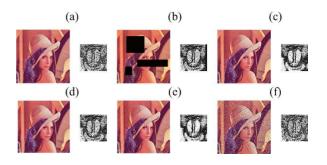


Fig. 5 Results of robustness experiment.

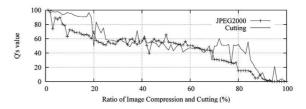


Fig. 6 JPEG2000 and cutting experiment.

where  $n = N/2^d$ ,  $d \in \{1, 2, \dots, \log_2(N-1)\}$ . f(i, j)and f'(i, j) are separately for the pixel at (i, j) of normal and extraction image with  $n \times n$  pixels.

Robustness test algorithm is defined in Equation (6). Q is robustness test value and  $Q \in [0, 1]$ . In the following experiments,  $\mu = \eta = 1$ . Expand Q 100 times to accommodate judgment habit.

$$Q = w\left(1 - p\right) \tag{6}$$

Figure 5 shows the result of different attacks such as JPEG2000 compression, cutting, filtering and noise.

Images are vulnerable to compression and cutting attacks, Figure 6 shows the Q' value corresponding to ratio of these attacks.

According to experiment, embedded information can be identified when Q reach about 30. Figure 5 and Figure 6 show that GHM-DCT is robust against JPEG2000 compression below 73%, cutting below 85%, common filtering and adding noise.

Experiment of ability against steganalysis. Higher order statistics detection algorithm based on wavelet coefficients (HOSWC) is a general detection algorithm [12]. Use the algorithms above-mentioned to analyze the performance of GHM-DCT. Experiment results are shown in Figure 7.

Experimental results of detection analysis to GHM-DCT using the High-order statistics detection based on wavelet coefficient (HOSWC) are shown in Figure 7. 100 random stego-images, we cant find one or even more threshold values. Using these detection methods, we obtain maximum detectable rate are respectively 3.91% and 3.64% which are very low.

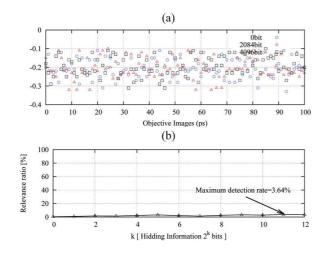


Fig. 7 Steganalysis experiment result of HOSWC to GHM-DCT.

Table 2 Detectable rate of attacks

JPEG2000	Cut	Filter	Gauss	saltpepper
99.25%	98.19%	99.57%	98.43%	99.85%

Table 3 Invisibility comparison based on PSNR

Algorithm	GHM-DCT	DWT-DCT	DWT-LSB
PSNR	36.8921	35.3270	935.9501

Experiments show the algorithm can resist these steganalysis.

Experiment of sensitivity to image attacks. Sensitivity to image attacks is the peculiar characteristic in GHM-DCT. Comparing  $R^L$  with  $R^H$  indicates the algorithm has excellent sensitivity of image processing. TABLE 2 lists the detectable rate when JPEG2000 compression ratio is 5%, random cutting ratio is 5%, [3,3] median filter, Gaussian ( $\mu = 0, \sigma^2 = 0.003$ ) and salt and pepper(d = 0.15). The average of detectable rate is 98.86%.

Experiment of invisibility comparison. According to PSNR, GHM-DCT has advantages in invisibility compared with DWT-DCT and DCT-LSB. Table 3 shows that invisibility increases by 3.51% averagely when embedding rate is 25%.

Experiment of robustness comparison. Figure 8, Figure 9 and Table 4 show robustness comparison results when embedding rate is 25% based on RTV.

The Q's value of GHM-DCT in JPEG2000 compression is 44.3492. DWT-DCT is 32.9980, and DCT-LSB is 42.6989. Indicate GHM-DCT is better robustness at JPEG2000. The Q's value of GHM-DCT in cutting is 57.3453. DWT-DCT is 33.7810, and DCT-LSB is 31.0311. Indicate GHM-DCT is better robustness at

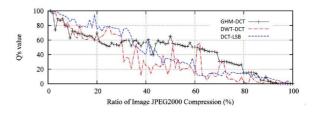


Fig. 8 Compression comparison.

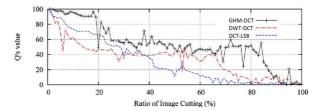


Fig. 9 Cutting comparison.

Table 4 RTV comparison of filtering and noise

Attacks	GHM-DCT	DWT-DCT	DWT-LSB
median filter	62.01	45.33	60.11
wiener2 filter	59.36	58.74	49.60
Gaussi	67.79	46.90	60.14
saltpepper	54.30	53.48	42.15

cutting. TABLE 4 show that GHM-DCT have better performance in robustness under filter and noise except compared with salt and peppe noise of DWT-DCT.

### **4** Conclusions

Propose an Information hiding scheme based on GHM and DCT. Take advantage of the energy distribution ratios the four sub-images after first-order GHM in multi-wavelet transformation, and use DCT to generate the DCT coefficients. Change the DCT coefficient to achieve information hiding. Chose  $LL_1$ , the energy of which accounts for 97.31% of the total image energy, as the algorithm hiding area. The feature of  $LL_1$  can meet the basic requirement of robustness hiding area. The energy feature of  $LH_2$  and  $HL_2$  can meet the basic requirement of invisibility hiding are. Choose high frequency DCT coefficients of  $LL_2$  component according to invisibility rule of DCT hiding area. Choose low frequency DCT coefficients of  $LH_2$  and  $LH_2$  according to robustness rule of DCT hiding are. The statistical properties of Chebyshev traverse and zero mean white noise are consistent [11], which is of good distribution and hiding characteristics to improve anti-steganalysis. Decompose  $HH_2$  according to 1 color space. Hide



information with LSB method in  $\beta$  components after gray-scaling which can meet the requirement of sensitivity and anti-steganalysis against common analysis based on LSB.

## **5** Acknowledgments

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