# An Efficient Firefly Algorithm for Optimizing Task Scheduling in Cloud Computing Systems

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**Abstract:** As user service demands change constantly, task scheduling becomes an extremely significant study area within the cloud environment. The goal of scheduling is distributing the tasks on available processors in order to achieve the shortest possible makespan while adhering to priority constraints. In heterogeneous cloud computing resources, task scheduling has a large influence on system performances. The various processes in the heuristic-based algorithm of scheduling will result in varied makespans when heterogeneous resources are utilized. As a result, a smart method of scheduling must be capable of establishing precedence efficacy for each task to decrease makespan time. In our study, we develop a novel efficient method of scheduling tasks according to the firefly algorithm to tackle an essential task and schedule a heterogeneous cloud computing problem. We evaluate the performance of our algorithm by putting it through three situations with changing amounts of processors and numbers of tasks. The findings of the experiment reveal that our suggested technique found optimal solutions substantially more frequently in terms of makespan time when compared with other methods.

**Keywords:** heterogeneous resources, firefly algorithm, task scheduling, cloud computing.
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## 1 Introduction

The distributed computing concept underpins the model of the cloud and consists of a collection of virtual machines that may be dynamically linked to build computing resources. Unutilized computing resources should be employed internationally to raise the rate of utilization and gain resources by improving their economic efficiency. The primary objective of the model of the cloud is to share users' data and resources. There are three forms of cloud computing: the first is IaaS, which refers to Infrastructure as a Service; the second is SaaS, which refers to Software as a Service; and the third is PaaS, which refers to Platform as a Service [1]. All of the services are available to users on a pay-as-you-go basis, and computing resources, applications, servers, networks, and data storage are shared. In a service SaaS, the licensed program is made available to the user on a subscription basis. The services can be accessed via a web browser from any device. In a service PaaS, the user can construct customized applications utilizing the services of the cloud and then publish them on their device. In a service IaaS, the client's organizational architecture is accessible online. The consumer is not required to comprehend the internal structure of the required infrastructure in order to use this service [1]. Rather than purchasing the complete corporate infrastructure, the consumer accepts only the necessary services as they are required. Because the number of cloud users has expanded in recent years, by default, the number of tasks that must be managed have increased for scheduling activities [1].

To address the issue of scheduling tasks more efficiently, we suggest a new approach based on the firefly algorithm to minimize the makespans of user requests on resources. Our Proposed Firefly Algorithm (PFA) minimizes makespans. In the firefly algorithm, the representation of a vector is a continuous value, so we use five manners that convert the continuous value to a discrete value. The priority is generated randomly to preserve the precedence constraints. These modifications improve the global optimization of the firefly algorithm's performance. We assess the performance of the PFA by putting it through three situations with changing amounts of processors and numbers of tasks. In terms of makespan, the results confirm that the PFA reaches the best solutions faster and more efficiently than other algorithms.

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The structure of this paper follows. The notations are provided in Section 2. Section 3 presents some related work on the task scheduling problem for various system architectures. The description of the issue of scheduling is presented in Section 4. The firefly algorithm is stated in Section 5. Our PFA is shown in Section 6. The results were obtained by applying the PFA and the comparisons with other results, as described in Section 7. The discussion is offered in Section 8, and Section 9 includes the conclusion of the paper and future work.

## 2 Notations

| | |
|---|---|
| $Tak_i$ | The Task i |
| $Pro_i$ | The Processor i |
| MPR | The Processor count |
| NTK | The task count |
| $CCO(Tak_i, Tak_j)$ | The cost between $Tak_i$ and $Tak_j$ |
| $STA(Tak_i, Pro_j)$ | $Tak_i$ start time on a $Pro_j$ |
| $FNT(Tak_i, Pro_j)$ | $Tak_i$ finish time on a $Pro_j$ |
| $RYT(Pro_i)$ | Ready time of the $Pro_i$ |
| LST | A list of jobs arranged in DAG topological order |
| $DATVE(Tak_i, Pro_j)$ | $Tak_i$ time of data arrival at $Pro_j$ |

## 3 Related Works

The cloud is a relatively new platform for managing and delivering internet-based services. This novel topic has recently received a great deal of interest from researchers. High efficiency in a cloud is the result of optimized task scheduling. Meta-inference methods of scheduling are often used where the scheduling of tasks are non-deterministic polynomial (NP) problems. A robust and optimized algorithm of genetics was presented by to improve the solutions [2]. The program combined the benefits of evolving genetic algorithms with experimental techniques.

Task scheduling is critical for scaling up dispersed electronic business systems and electronic science systems. This usage typically includes the communication of tasks that are performed on virtual resources or virtual machines. The basic goal of any scheduling approach is to decrease the breadth of the configuration, which represents the makespan of the exit job. A model called H3CSA was proposed in this regard [3].

Cloud service providers provide diverse virtual computers to conduct complicated tasks designated by consumers. A meta-hybrid method that used a genetic algorithm and thermodynamic simulated annealing algorithms (GATSA) was presented to solve the problem; the global and local search tendencies of the two algorithms compensated for each other's weaknesses. A novel theory was introduced and used to generate a semi-conducted starting population [4].

Proper task scheduling is necessary for optimal efficiency in cloud computing; however, traditional experimental methods in this context lack the necessary efficiency because task scheduling in a cloud is entirely NP. As a result, the bulk of recently suggested task scheduling methods have concentrated on a hybrid descriptive technique of job scheduling. A meta-heuristic technique algorithm known as HEFT was proposed [5].

Other researchers suggested inferential algorithms such as the ICA and FA to tackle the issue. Although ICA and FA can approach reasonable solutions, scalability, time of CPU, stability, and balancing of load are necessary to attain the most effective outcomes. A smart method that is based on the marriage of FA and ICA to obtain the desired result was proposed; FA's local search can enhance the ICA [6].

A new strategy was proposed to overcome the challenge of scheduling resources in cloud computing; it employed a model that improved the parallel scheduling of tasks while maintaining the relationships between serial tasks [7]. The primary characteristic of dynamic tasks was that users could assign varied and equal priorities to activities performed in sequential order and arrange them in a scheduling queue. FA was utilized for scheduling subtasks to show improvement in a short amount of time. The most critical factors to evaluate were fairness and efficiency; the strategy known as DSFFA was used to solve the task scheduling problems.

The scheduling of tasks is a primary concern within the cloud to prevent diminished system performance. A significant method that organizes the requirements of the user and achieves several aims, the technique aims to lessen the workload makespan and the cost of execution while increasing resource usage [8].

## 4 Problem Descriptions

During this work, the task scheduling model is delineated as distributed NTK's to be implemented on MPR processors that may be different. A task graph is mapped to describe the problem structure—a DAG composed of NTK's $Tak_1$, $Tak_2$, $Tak_3$, …$Tak_n$. Every node of the graph is identified as a task. We know that a task is a series of instructions that are implemented by the processor in successive order. A task may have pre-requested data; once all the inputs needed for the execution are received, the task can be put into the processor for implementation. These inputs are intended to be supplied after the completion of certain other activities, as these tasks assess them. We refer to this as relying on task dependency. If a task (t) is dependent on data from other tasks, then those tasks are recognized as the fathers of the task (t), and task (t) is their child. A task that has no father is called an "entry task," and a task that has no child is called an "exit task" [9]. The computing cost of a job is based on its execution time. Whenever the cost of computation of a $Tak_i$ is indicated by weight $(Tak_i, Pro_j)$, the DAG has additional edges that represent a partial order between the tasks. The partial order between the tasks introduces constrained precedence in a DAG such that if $Tak_j$ is a child of $Tak_i$ ($Tak_i \rightarrow Tak_j$), it cannot begin its execution until its father $Tak_i$ finishes its execution. The value on the edge represents the cost of communication between the tasks and is indicated by $CCO(Tak_i, Tak_j)$. The communication cost is considered only if $Tak_i$ and $Tak_j$ are assigned to different processors; otherwise, it is calculated to be zero. In that case, $Tak_i$ and $Tak_j$ are given to the processor itself. If a $Tak_i$ is given to $Pros_j$, the task's start and finish times are denoted by $STA(Tak_i, Pro_j)$ and $FNT(Tak_i, Pro_j)$, respectively. After scheduling the tasks, the makespan is defined as max $\{FNT(Tak_i, Pro_j)\}$ throughout all processors. The problem of scheduling tasks involves coordinating the schedules of the tasks in the different processors, decreasing the makespan for all of those schedules, and ensuring that the task dependency constraints are preserved. Task dependency constraints state that no task can begin before all fathers have terminated. Assuming that $Pro_j$ is the processor and that the $KP^{th}$ parent task $Tak_{kp}$ of task $Tak_i$ is scheduled, the DATVE of $Tak_i$ at processor $Pro_j$ is when the prerequisite data for the task execution becomes available. This is defined in [9] by the following:

$$DATVE(Tak_i, Pro_j) = max\{FNT(Tak_{kp}, Pro_j) + CCO(Tak_i, Tak_{kp})\} \qquad (1)$$
where $kp = 1,2, 3, ….$ Parent Number

$$STA(Tak_i, Pro_j) = max\{RYT(Pro_j), DATVE(Tak_i, Pro_j)\} \qquad (2)$$

$$FNT(Tak_i, Pro_j) = STA(Tak_i, Pro_j) + weight(Tak_i, Pro_j) \qquad (3)$$

$$RYT(Pro_j) = FNT(Tak_i, Pro_j) \qquad (4)$$

$$Makespan = max\{FNT(Tak_i, Pro_j)\} \qquad (5)$$

## 5 Firefly Algorithms

Yang [10] created the firefly algorithm, which was modeled on the motion of flashing fireflies. For the sake of simplicity, we incorporate this concept into the rules listed below:

- Because all fireflies are unisex, all fireflies are attracted to all other fireflies.

- Their appeal is related to their luminosity. As a result, when two fireflies are flashing, the one with the lower brightness will move toward the one that is brighter. The attraction is based on the brightness, which decreases as the distance between the objects increases. If no firefly is brighter, the firefly moves randomly.

- The goal function's landscape to be optimized influences or determines the brightness of a firefly or the ferocity of a firefly.

There are two major concerns in the FA: the modulation of the intensity of light, and the creation of appeal. In the simplest example of the greatest improvement issue, the brightness IB of a firefly at a given position y will be selected as IB(y) α g(y). However, the attractiveness $\delta$ is subjective; it must be viewed according to the other firefly. As a result, it must change depending on the $R_{ij}$, which is the separation between fireflies i and j. The intensity of light diminishes in relation to the distance from the source, and light is also absorbed inside the medium. That is:

$$IB = IB_0 exp(-\varphi R) \qquad (6)$$

where $IB_0$ represents the initial brightness of the light and $\varphi$ is the coefficient of light absorption. The attractiveness of a firefly is shown by:

$$\delta = \delta_0 \exp(-\varphi R^2) \tag{7}$$

A firefly i's attraction to a more attractive firefly j is determined by:

$$y_i = y_i + \delta_0 \exp(-\varphi R_{ij}^2)(y_j - y_i) + \alpha\varepsilon_i \tag{8}$$

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**Firefly Algorithm**

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$g(y)$ is the objective function where $y = (y_1, ..., y_d)^T$

Initialize a firefly's $y_i$ where i is equal from 1 to n

The $IB_i$ is computed by using $g(y_i)$

While (iteration <Maximum of generation)

{

For i equal 1 to n

  {

   For j equal 1 to i

    {

     If ($IB_j > IB_i$)

      {

      The firefly(i) should be moved to j in all dimensions.

      }

     Through $\exp[-\varphi R]$

     Update the intensity of the light and evaluate newly discovered solutions

     }

   }

To find current best, rank fireflies

}

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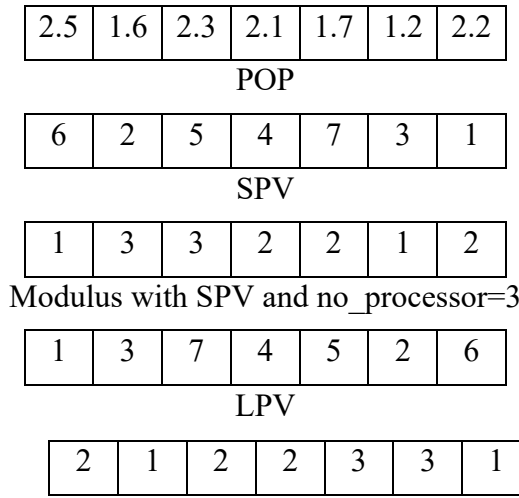
## 6 The Proposed Algorithm

PFA begins with the first set of initializations. Then, by applying some operators, the best solution is chosen according to the value of the goal function. In PFA, we state the following steps:

### 6.1 Initialization

The initialization is randomly generated according to this equation:

$$POP_{ij} = LB + rand*(UB - LB) \tag{9}$$

Where UB and LB refer to the upper and lower boundaries, we consider that the value of the UB is equal to the number of processors and the LB value is equal to one. Because the representation of a vector is a continuous value, we will use the LPV rule [11] and the SPV rule [12], as shown in Figure 1.

| 2.5 | 1.6 | 2.3 | 2.1 | 1.7 | 1.2 | 2.2 |
|---|---|---|---|---|---|---|

POP

| 6 | 2 | 5 | 4 | 7 | 3 | 1 |
|---|---|---|---|---|---|---|

SPV

| 1 | 3 | 3 | 2 | 2 | 1 | 2 |
|---|---|---|---|---|---|---|

Modulus with SPV and no_processor=3

| 1 | 3 | 7 | 4 | 5 | 2 | 6 |
|---|---|---|---|---|---|---|

LPV

| 2 | 1 | 2 | 2 | 3 | 3 | 1 |
|---|---|---|---|---|---|---|

Modulus with LPV and no_processor=3

**Fig.1:** An example of the proposed schedule.

## 6.2 Priority Operations

Task prioritization plays a big role in task scheduling and calculating the makespan. The proposed priority is randomly generated in order to preserve the precedence constraints.

## 6.3 The Objective Function

The scheduling problem's primary goal is to lower the makespan, which is calculated according to equation 5. That is:

Objective Function = Makespan                                                             (10)

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**Algorithm 1:** Calculate the makespan of the scheduled task using the Standard Genetic Algorithm (SGA) [9]

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Input the schedule of tasks as shown in Figure 1

Output objective function

$RYT[Pro_j] = 0$             where     $j = 1, 2, \ldots\ldots MPR$.

For $i = 1$ to NTK

{

    // LST is generated randomly in an order that preserves precedence constraints

    Take the first $Tak_i$ from LST

    For $j$ equal 1 to MPR

      {

    If $Tak_i$ scheduled to $Pro_j$

      {

     Calculate start time according to equation 2

     Calculate finish time according to equation 3

     Calculate ready time according to equation 4

      }

}

}

Calculate makespan according to equation 5

Calculate the objective function according to equation 10

## 6.4 The Proposed Operations

**Algorithm 3:** The whole PFA

Input the DAG with computation cost and communication cost

Output the best solution

Initialize the parameters $\alpha$, $\delta_0$, $\varphi$, $\partial$, N, max_iteration

Generate the initial population according to equation 9

Convert a continuous value to a discrete value by using **Algorithm 2**

Calculate the objective function $g(y_i)$ by using **Algorithm 1**

For iteration=1 to max_iteration

{

　For i equal 1 to N

　{

　　For j equal 1 to N

　　　{

　　　If ( $g(y_i) > g(y_j)$)

　　　　{

　　　　Update the location using equation 8

　　　　Convert a continuous value to a discrete value of the new solution by using **Algorithm 2**

　　　　Compute the makespan of the newly obtained solution by using **Algorithm 1** and update it if better

　　　　}

　　　}

　}

}

**Algorithm 2:** The algorithm that transforms continuous values into discrete values.

Function Convert (s)

A = random number between  [1…5]

If  (A==1)

　　Use the SPV rule

Else if (A==2)

　　Use the LPV rule

Else if (A==3)

Use the round nearest function

Else if (A==4)

Use the floor nearest function

Else

Use the ceil nearest function

End if

End function

## 7 Evaluation of the PFA

We show the effectiveness of the PFA by applying it to three cases. The first case consists of ten tasks and three heterogeneous processors. The second case consists of ten tasks and three heterogeneous processors. The third case consists of eleven tasks and three heterogeneous processors. PFA was implemented as a system by MATLAB 2016. We set the values of the initial parameters $\alpha = 1.0$, $\delta_0 = 1.0$, $\varphi = 0.01$, $\partial = 0.97$, N = 30, max_iteration = 50.

### 7.1 Case 1

Suppose we have ten tasks to be executed on three heterogeneous processors $\{Pro_1, Pro_2, Pro_3\}$. The executing cost of each task is shown in [3]. The best solution obtained by PFA is shown in Figure 2, and the schedule obtained by PFA and other algorithms is shown in Table 1. The outcomes of the PFA are compared with those obtained by the New Genetic Algorithm (N-GA) [2], Proposed Particle Swarm Optimization (PPSO) [13], and H3CSA [3]. The obtained results are illustrated in Table 2 and Figure 3 with the proposed task priority of PFA $\{Tak_1, Tak_4, Tak_3, Tak_2, Tak_6, Tak_7, Tak_5, Tak_9, Tak_8, Tak_{10}\}$, task priority of N-GA $\{Tak_1, Tak_4, Tak_2, Tak_3, Tak_7, Tak_5, Tak_6, Tak_9, Tak_8, Tak_{10}\}$, task priority of PPSO $\{Tak_1, Tak_2, Tak_3, Tak_4, Tak_5, Tak_6, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, and task priority of H3CSA $\{Tak_1, Tak_4, Tak_3, Tak_7, Tak_6, Tak_2, Tak_5, Tak_9, Tak_8, Tak_{10}\}$.

| 1 | 1 | 1 | 1 | 2 | 3 | 1 | 2 | 3 | 2 |
|---|---|---|---|---|---|---|---|---|---|
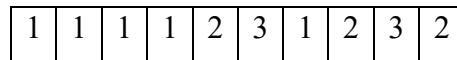
**Fig. 2:** The best solution for case 1.

**Table 1:** Schedule obtained by PFA and other algorithms for case 1.

|  | N-GA | | | PPSO | | | H3CSA | | | PFA | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
|  | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 |
| Tak$_1$ |  |  | 0–4 | 0–7 |  |  | 0–7 |  |  | 0–7 |  |  |
| Tak$_2$ |  |  | 32–50 | 7–14 |  |  | 36–43 |  |  | 30–37 |  |  |
| Tak$_3$ | 43–60 |  |  | 14–31 |  |  | 13–30 |  |  | 13–30 |  |  |
| Tak$_4$ |  |  | 4–32 | 31–37 |  |  | 7–13 |  |  | 7–13 |  |  |
| Tak$_5$ |  | 61–78 |  |  | 32–49 |  |  | 54–71 |  |  | 48–65 |  |
| Tak$_6$ |  |  | 62–89 | 37–72 |  |  |  |  | 33–60 |  |  | 33–60 |
| Tak$_7$ | 60–66 |  |  | 72–78 |  |  | 30–36 |  |  | 37–43 |  |  |
| Tak$_8$ | 113–133 |  |  | 84–104 |  |  |  | 79–119 |  | 79–119 |  |  |
| Tak$_9$ |  |  | 97–113 |  | 109–142 |  |  |  | 75–91 |  |  | 74–90 |
| Tak$_{10}$ |  | 163–175 |  |  | 142–154 |  |  | 124–136 |  |  | 123–135 |  |

**Table 2:** Comparative results based on case 1.

| Algorithm | N-GA | PPSO | H3CSA | PFA |
|-----------|------|------|-------|-----|
| Makespan | 175 | 154 | 136 | 135 |
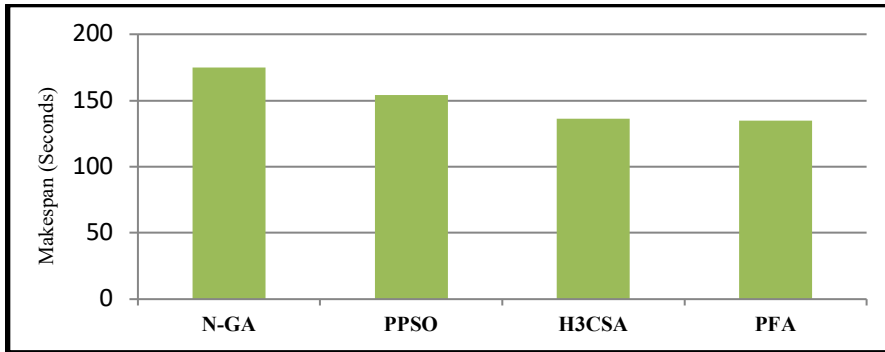


**Fig. 3:** Comparison of results for case 1.

## 7.2 Case 2

Suppose we have ten tasks to be executed on three heterogeneous processors $\{Pro_1, Pro_2, Pro_3\}$. The executing cost of each task is shown in [9]. The best solution obtained by PFA is shown in Figure 4, and the schedule obtained by PFA and other algorithms is shown in Table 3. The outcomes of the PFA are compared with those obtained by the WOA [14], GSA [15], Simulated Annealing (SA), GA, EGA-TS [16], Genetic Algorithm (GA) [8], and Hybrid Heuristic and Genetic (HHG) [17]. The obtained results are illustrated in Table 4 and Figure 5 with the proposed task priority of PFA $\{Tak_1, Tak_6, Tak_4, Tak_5, Tak_2, Tak_3, Tak_8, Tak_9, Tak_7, Tak_{10}\}$, task priority of WOA $\{Tak_1, Tak_3, Tak_5, Tak_2, Tak_4, Tak_6, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, task priority of SA $\{Tak_1, Tak_5, Tak_3, Tak_2, Tak_4, Tak_6, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, task priority of EGA-TS $\{Tak_1, Tak_3, Tak_5, Tak_2, Tak_4, Tak_6, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, task priority of GSA $\{Tak_1, Tak_3, Tak_2, Tak_6, Tak_4, Tak_5, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, task priority of GA $\{Tak_1, Tak_3, Tak_2, Tak_6, Tak_4, Tak_5, Tak_7, Tak_8, Tak_9, Tak_{10}\}$, task priority of GA $\{Tak_1, Tak_2, Tak_4, Tak_5, Tak_9, Tak_3, Tak_7, Tak_6, Tak_8, Tak_{10}\}$, and task priority of HHG $\{Tak_1, Tak_2, Tak_6, Tak_3, Tak_4, Tak_5, Tak_8, Tak_7, Tak_9, Tak_{10}\}$.

| 2 | 2 | 2 | 1 | 3 | 1 | 2 | 1 | 3 | 1 |
|---|---|---|---|---|---|---|---|---|---|
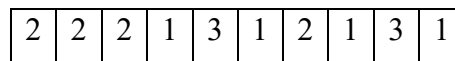
**Fig. 4:** The best solution for case 2.

**Table 3:** Schedule obtained by PFA and other algorithms for case 2.

| | WOA | | | SA | | | EGA-TS | | | GSA | | | GA | | | GA | | | HHG | | | PFA | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 |
| Tak₁ | | 0 – 21 | | | 0 – 21 | | | 0 – 21 | | | 0 –21 | | | 0 –21 | | | 0 – 22 | | | 0 – 21 | | | 0 – 21 | |
| Tak₂ | | | 38 – 56 | | | 38 – 56 | | 38 – 60 | | | | 38 – 58 | | | 38 – 58 | | 22 – 44 | | | 21 – 39 | | | 21 – 39 | |
| Tak₃ | | 21 –48 | | | 21 –48 | | | 21 – 48 | | | 21 – 48 | | | 21 – 48 | | | 44 – 76 | | | 39 – 66 | | | 39 – 66 | |
| Tak₄ | | 48 –58 | | | 48 –58 | | | 48 – 58 | | 50 – 57 | | | 50 – 57 | | | | 51 –61 | | | | 50 – 54 | 64 –71 | | | |
| Tak₅ | 34 – 63 | | | 34 – 63 | | | | | 34 – 69 | | 56 – 91 | | | 56 – 91 | | | 35 – 70 | | | 54 – 89 | | | | 34 – 69 |
| Tak₆ | | 58 | | | 58 | | | 58 | | | 48 | | | 48 | | | 61 | | 38 | | | 38 | | |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| | −75 | −75 | −75 | −65 | −65 | −78 | −64 | −64 |
| Tak7 | 64−78 | 64−78 | 75−100 | 64−78 | 64−78 | 76−90 | 66−91 | 66−91 |
| Tak8 | 75−98 | 75−98 | 80−109 | 68−91 | 68−91 | 78−101 | 65−94 | 71−100 |
| Tak9 | 86−101 | 86−101 | 90−98 | 91−99 | 91−99 | 74−82 | 89−97 | 78−86 |
| Tak10 | 108−124 | 108−124 | 109−122 | 106−122 | 106−122 | 101−117 | 104−117 | 100−113 |

**Table 4:** Comparative results based on case 2.

| Algorithm | WOA | SA | EGA-TS | GSA | GA[5] | GA[9] | HHG | PFA |
|---|---|---|---|---|---|---|---|---|
| Makespan | 124 | 124 | 122 | 122 | 122 | 117 | 117 | 113 |
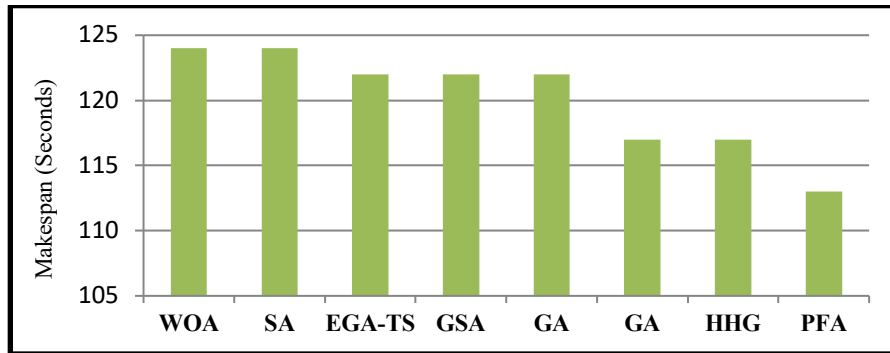


**Fig. 5:** Comparison of results for case 2.

## 7.3 Case 3

Suppose we have eleven tasks to be executed on three heterogeneous processors {Pro1, Pro2, Pro3}. The executing cost of each task is shown in [18]. The best solution obtained by the PFA is shown in Figure 6, and the schedule obtained by the PFA and other algorithms is shown in Table 5. The outcomes of the PFA are compared with those obtained by three heuristic HEFT algorithms. MPQMA [18]. The obtained results are illustrated in Table 6 and Figure 7 with the proposed task priority of PFA {Tak0, Tak2, Tak1, Tak3, Tak4, Tak6, Tak5, Tak7, Tak8, Tak9, Tak10}, task priority of HEFT-T {Tak0, Tak4, Tak2, Tak3, Tak1, Tak5, Tak6, Tak7, Tak8, Tak9, Tak10}, task priority of HEFT-B {Tak0, Tak4, Tak3, Tak2, Tak1, Tak7, Tak6, Tak5, Tak9, Tak8, Tak10}, task priority of HEFT-L {Tak0, Tak3, Tak4, Tak2, Tak1, Tak7, Tak6, Tak5, Tak9, Tak8, Tak10}, task priority of MPQMA {Tak0, Tak1, Tak2, Tak5, Tak3, Tak4, Tak7, Tak9, Tak6, Tak8, Tak10}.

| 2 | 3 | 1 | 2 | 2 | 1 | 1 | 2 | 1 | 2 | 1 |
|---|---|---|---|---|---|---|---|---|---|---|
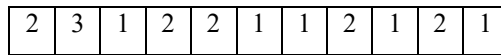
**Fig. 6:** The best solution for case 3

**Table 5:** Schedule obtained by PFA and other algorithms for case 3.

| | HEFT-T | | | HEFT-B | | | HEFT-L | | | MPQMA | | | PFA | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 | 1 | 2 | 3 |
| Tak0 | | | 0–5 | | | 0–5 | | | 0–5 | | | 0–5 | | 0–7 | |

| | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Tak1 | | | 22–30 | | 23–32 | | | | 20–28 | | | | 5–13 | | | 25–33 |
| Tak2 | | | 15–22 | 19–27 | | | 19–27 | | | | | 13–20 | 21–29 | | |
| Tak3 | 20–31 | | | | | 15–30 | | | 5–20 | 20–31 | | | | | 7–20 | |
| Tak4 | | | 5–15 | | | 5–15 | | 16–23 | | | 16–23 | | | | 20–27 | |
| Tak5 | | | 30–38 | | 37–47 | | | | 37–45 | | | 20–28 | 47–53 | | |
| Tak6 | | 39–51 | | 27–45 | | | 27–45 | | | | | 28–43 | 29–47 | | |
| Tak7 | 40–57 | | | | | 30–42 | | 38–48 | | | 49–59 | | | 27–37 | |
| Tak8 | | 52–72 | | | | 61–72 | | | 56–67 | | | 43–54 | 53–67 | | |
| Tak9 | 57–69 | | | | | 42–52 | | 48–56 | | | 59–67 | | | 37–45 | |
| Tak10 | 85–94 | | | | | 72–89 | | 80–89 | | | 67–80 | | 67–76 | | |

**Table 6:** Comparative results based on case 3.

| Algorithm | HEFT-T | HEFT-B | HEFT-L | MPQMA | PFA |
|---|---|---|---|---|---|
| Makespan | 94 | 89 | 89 | 80 | 76 |
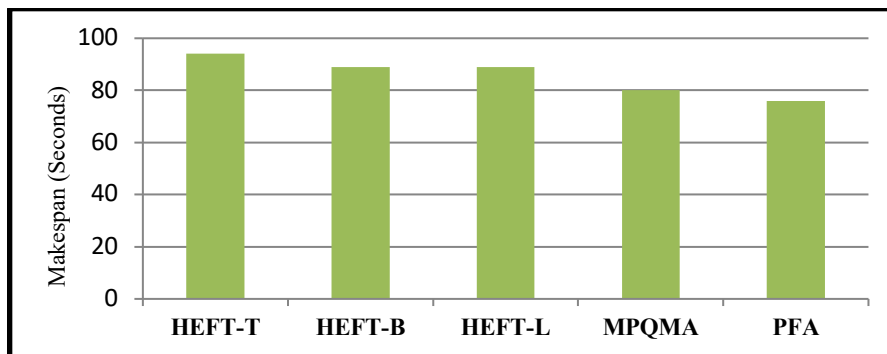


**Fig.7:** Comparison of results for case 3.

## 8 Discussions

The outcomes in Figure 3 and Table 2 show that the makespan of the PFA is reduced by (22.85%), (12.33%), and (0.73%) for N-GA, PPSO, and H3CSA, respectively. The outcomes in Figure 5 and Table 4 show that the makespan of the PFA is reduced by (8.87%), (8.87%), (7.37%), (7.37%), (3.41%), and (3.41%) for WOA, SA, EGA-TS, GSA, GA, and HHG, respectively. The outcomes in Figure 7 and Table 6 show that the makespan of the PFA is reduced by (19.14%), (14.60%), (14.60%), and (5%) for HEFT-T, HEFT-B, HEFT-L, and MPQMA, respectively.

## 9 Conclusions and Future Work

In order to achieve near-optimal results for the issue of scheduling tasks in a cloud, efficient strategies for the optimal mapping of the tasks are required. In this study, we suggest a novel efficient scheduling task method in the cloud that uses the firefly algorithm to address the issue of scheduling tasks. The system is made up of a small number of fully linked heterogeneous virtual machines. The method has been compared to other algorithms according to makespan. The comparative analysis illustrates that the PFA is significantly better in all cases. In our future work, we will develop an efficient algorithm to tackle scheduling tasks in a cloud using the algorithm of cuckoo search.

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