Modeling and Analyzing Neural Networks Using Reproducing Kernel Hilbert Space Algorithm

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Abstract: In this paper, we present a new method for solving some certain differential systems in the artificial neural networks field. The analytic and approximate solutions are given with series form in the spaces W[a,b] and H[a,b]. The method used in this thesis has several advantages; first, it is of global nature in terms of the solutions obtained as well as its ability to solve other mathematical, physical, and engineering problems; second, it is accurate, need less effort to achieve the results, and is developed especially for the nonlinear cases; third, in the proposed method, it is possible to pick any point in the interval of integration and as well the approximate solutions will be applicable; fourth, the method does not require discretization of the variables, and it is not affected by computation round off errors and one is not faced with necessity of large computer memory and time. Results presented in this thesis show potentiality, generality, and superiority of our method as compared with the Range Kutta method.

Keywords: Reproducing kernel algorithm; Artificial neural networks; differential systems

1 Introduction

Artificial neural networks (ANN) are consisting of group from the virtual neurons that designed by computerized programs which use a various of mathematical fractional equations. These equations put in the hidden layers to process the data that comes from the neurons. The ANN we can call it also simulated neural networks SNN because the ANN simulate the mechanism of the biological neural networks, its consist of nodes may be processing elements or neurons. Every connection between the nodes has a weight and by these weights of connections we can define the produced values of each node by calculate the weights values that of each connection that comes to the specific node. By brief words the ANN is a programmed attempt to simulate the way the human brain work and the appendages of nerve bound the nerve cells to build the neural networks in the human brain. The human brain has a millions of the connected nerve cells, the ANN able to allow human mental activities like:

1. The ability of store the information.
2. The ability to sense, hearing, taste and smell.
3. Learning many things.
4. Distinguish between the things and decision making.
5. The possibility of remembering the shapes, colors, the pictures, and people.

For example, to learn specific type of smart phones we will save in our mind the shape of phone its features, its color, its type, and its size. This is an allowed activity of neural networks and we can remember all of these features by also ANN.

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1. Components of the artificial neurons

Every neuron consists of three elements:
1. Weights: each neuron has a weight expressed as a real number and according to these weights of each neuron we can determine the strength of neurons contribution.
2. Weighted Sum: its a summation of all the income weights to the specific neuron thats come from other neurons. In ANN this factor will help in trying to gather a best set of the income weights values for each neuron to know which the neuron has real and useful values that comes from specific action issued by the neurons.
3. Activation Factor: when the neuron gives some action for another one. The issued neuron for this action will send it by signal to the activation factor which would express this signal as an exponential relation to process this signal to get the final result.

The human brain able to process the inputs or givens, so that every part of the brain has a specific function and implement some task. Its called plasticity to simulate the computer thats consists of multiprocessor and each of the will execute task which called parallel computing.

1.2 The weights and the weighted matrix in ANN

As we said the technical neural network consist of many connected neurons or processing units that associate with each other to exchange the information by connections. Each of these connections has a weight, and its called connection weight. For example, we have two connected neurons the connection weight of them will be expressed as $W_{ij}$. We can represent the weight in weight matrix or in weight vector; the number of rows in the matrix weight determines the cell that carried out the connection to the target cells or to the desired cells to receive information that is sent. In other words, from the row number we can identify from any neuron the connection begins between two neurons, and by the column number determines receptor neurons to the information or signals. In case of the column number was equal zero this means no connection exist, this matrix also called Hinton diagrams.

1.3 Mechanism of Artificial Neural Networks

In this section, summed up the work of the mechanism of ANN in data processing across three stages and each stage outputs are input to the next stage, respectively, and we will show this on example form. Stages of information processing are as follows:
1. Propagation function stage
2. Activation function stage
3. Output function stage

1.4 Network Topologies

1. After we became familiar with the nerve cell combination, here we will give an overview about the famous topologies of the neural networks to construct neural network that consists of the previous components we will firstly decide what will be the based topology of the network that we will describe it with its map on diagram to enable the reader understanding the features and its approach on the neural networks.
2. In the Hinton diagram the dotted weights expressed as a gray field, the solid weights are expressed as a dark gray field. the input and output arrows added to identify the sent neuron by put its name as a line and the destination neuron will be as a column number or column name.

1.5 learning procedures by input training patterns

The purpose of the neural networks to predict to make the input patterns as a common form by training procedure which called generalization. Here in this section we will propose some of the learning procedures and give some of the basic principles to learning procedures approaches [1]. Firstly, we will preview the operations that the neural networks can do them such as:
1. The neural networks can develop a new connections or create them between the neurons and as we said its called weighted connection. Later on we will explain how we can set the weight value to reduce the difference value between the desired outputs and the current outputs to give a good result.
2. The neural network can delete an exist connection between the neurons by put the connected weight value in the weighted matrix between the connected neurons as we learned zero value to cancel the connection.
3. The neural network can change the connected weight value by specific rules they will be explained later on.
4. The neural network able to change the threshold value of the neurons.
5. The neurons in the neural network able to implement a main task (propagation function, activation function and output function).
6. The neural network can add or delete neurons.

The neural network form characterized by their ability to predict the solutions that fit the problem in accurate form. For example, in the medicine domain by input the symptoms of the disease and then by processing the information by the neural networks it will predict the disease or diagnosis of the disease. Another example when give the neural network input patterns we will predict of it to give the desired pattern or desired output.
This could be executed by the training of the network by using an input pattern training to train the network give the desired output by learning algorithms:

### 1.6 Hopfield Neural Networks

This type of the wide domain of artificial neural networks is same idea or the Hopfield neural network come from idea that the particles which situated in magnetic domain and each of these particles is connect via the magnetic force with all the particles in the domain in completely linked or in other words in fully connected form. So we will apply the previous topology of the neural network which means completely linked topology. We can say about the particle is neuron and these particles when they connect as a fully connected with each other to try to become their activation states are suitable and we can know the minimum activation of the neurons or particles by themselves. When the Hopfield network neurons will be in rotating state they will encourage each other to spin this idea the rotation of the particles is to process the information which means they will be in the activation case. For example, if we have a two particles are in rotating state to process the information this called in the Hopfield neural networks is binary activation [2].

### 1.7 Problem Statement

Let us consider the following theorem that summarize our work:

**Theorem 1.1.** [3, 4, 5, 6] If there exist a number \( L > 0 \) such that \( \| h(s_1) - h(s_2) \| \geq L \| s_1 - s_2 \| \) for all \( s_1, s_2 \in \mathbb{R}^n \) and the number \( \epsilon \) is sufficiently small, then there exists a neighborhood \( N \) of the orbitally stable limit cycle of the equation \( u' = -Du + W g(u) \) such that the solutions of the equation \( u' = -Du + W g(u) + \epsilon h(x(t)) \) which start inside \( N \) behave chaotically around the limit cycle, that is the solutions are sensitive and there are infinitely many unstable periodic solutions.

To illustrate the result of the above theorem, let us consider the following general HNN:

\[
\begin{align*}
\dot{x}_1 &= f_1(t, x_1, x_2, \ldots, x_n), T \in t, \\
\dot{x}_2 &= f_2(t, x_1, x_2, \ldots, x_n), T \in t, \\
&\quad \vdots \\
\dot{x}_n &= f_n(t, x_1, x_2, \ldots, x_n), T \in t,
\end{align*}
\]

subject to the following initial conditions:

\[
\begin{align*}
x_1(0) &= \alpha_1, \\
x_2(0) &= \alpha_2, \\
&\quad \vdots \\
x_n(0) &= \alpha_n,
\end{align*}
\]

over the long interval \( T = [a, b] \). In fact, the above system consists of several cases on the Hopfield neural network.

### 2 Reproducing Kernel Hilbert Spaces Method

The theory of reproducing kernel was used for the first time at the beginning of the 20th century as a novel solver for the boundary value problems of harmonic and biharmonic functions types. This theory, which is representative in the reproducing kernel Hilbert spaces (RKHS) method, has been successfully applied to various important application in numerical analysis, computational mathematics, image processing, machine learning, probability and statistics, and finance [7, 8, 9, 10]. The RKHS method is a useful framework for constructing numerical solutions of great interest to applied sciences. In the recent years, based on this theory, extensive work has been proposed and discussed for the numerical solutions of several integral and differential operators side by side with their theories. The reader is kindly requested to go through [11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35] in order to know more details about the RKHS method, including its modification and scientific applications, its characteristics and symmetric kernel functions, and others.

#### 2.1 Multistep Approach

The major aim of this work is to find the approximate solutions over along interval. In this section, we utilize the multistep RKHS procedure. To do so, we consider the nonlinear differential equations of Eqs. (2.1) and (2.2). Indeed, let \( T = [a, b] \) be the interval over which we want to find the solution. Assume that the interval \( T \) is divided into \( M \) subintervals \([\beta^{m-1}, \beta^{m}]\), \( m = 1, 2, \ldots, M \) of equal step size \( h = \frac{b - a}{M} \), by using the nodes \( \beta^m = mh \). Firstly, we apply the RKHS method over the interval \([a, \beta^1]\), to obtain the approximate solution. For \( m \geq 2 \) and at each subinterval \([\beta^{m-1}, \beta^m]\), we will use the initial conditions obtained over \([a, \beta^1]\), then apply the RKHS technique directly. The process is repeated and generates a sequence of approximate solutions over \([a, \beta^1], [\beta^1, \beta^2]\), and \([\beta^{m-1}, \beta^m]\).
2.2 Computational RKHS Algorithm

Software packages have great capabilities for solving mathematical, physical, and engineering problems. The aim of the next algorithm is to implement a procedure to solve system of differential equations in numeric form in terms of their grid nodes based on the use of RKHS method.

Algorithm 1 To approximate the solution \( x^h(t) \) of \( x_i(t) \), we do the following steps:

**Input:** The endpoints of \([a,b]\), the unit truth interval \([0,1]\), the integers \( n \) and \( m \), the kernel functions \( G_i(s) \) and \( H_i(s) \), the differential operator \( L_x \), the initial condition \( \alpha \), and the function \( f_r \).

**Output:** Approximate solution \( x^h(t) \) of \( x_i(t) \).

**Step i.** Fixed \( t \) in \([a,b]\) and set \( s \in [a,b] \);
If \( s \leq t \), set
\[
G_i(s) = \frac{1}{6} (s-a)(2a^2 - s^2 + 6t + 3s - a(6 + s + 3t));
\]
else set
\[
G_i(s) = \frac{1}{6} (t-a)(2a^2 - t^2 + 3s(2 + t) - a(6 + 3s + t));
\]
For \( i = 1, 2, \ldots, n \) and \( j = 1, 2, \ldots, n \), do the following:
Set \( t_i = \frac{t - 1}{n - 1} \); Set \( \psi_{ij}(t) = L_x[G_i(s)]s = t_i \);

**Output:** the orthogonal function system \( \psi_{ij}(t) \).

**Step ii.** For \( l = 2, 3, \ldots, n \) and \( k = 1, 2, \ldots, l - 1 \), do the following:
If \( k \neq l \) then set
\[
\beta_{lk}^{ij} = \frac{-\sum_{p=1}^{l-1} \langle \psi_{lk}(t), \psi_{ij}(t) \rangle w \beta_{pk}^{ij}}{\| \psi_{lk} \|_w^2 - \sum_{p=1}^{l-1} \langle \psi_{lk}(t), \psi_{ij}(t) \rangle _w^2};
\]
else set
\[
\beta_{lk}^{ij} = \frac{1}{\| \psi_{lk} \|_w^2};
\]
else set
\[
\beta_{11}^{ij} = \frac{1}{\| \psi_{11} \|_w};
\]

**Output:** the orthogonalization coefficients \( \beta_{lk}^{ij} \).

**Step iii.** For \( l = 2, 3, \ldots, n \) and \( k = 1, 2, \ldots, l - 1 \), do the following:
Set \( \psi_{ij}(t) = \sum_{l=1}^{n} \sum_{j=1}^{l} \beta_{lk}^{ij} \psi_{lk}(t) \);

**Output:** the orthonormal function system \( \psi_{ij}(t) \).

**Step iv.** Set \( x^0_{r_0}(t_1) = x_{1, r_0}(t_1) = 0 \);
Set \( B_{ij} = \sum_{j=1}^{l-1} \sum_{l=1}^{n} \beta_{lk}^{ij} f_k(t_i, x^{l-1}(t_l)) \);
Set \( x^l(t) = \sum_{i=1}^{l} \sum_{j=1}^{l} B_{ij} \psi_{ij}(t) \);

**Output:** the approximate solution \( x^h(t) \) of \( x(t) \).

**Step v.** Stop.

3 Numerical Simulation

In order to solve the given ANN problems numerically on a computer, the equation is approximated by a discrete one. Continuous functions are approximated by finite arrays of values. Algorithms are then sought which approximately solve the mathematical problem efficiently and accurately. To show behavior, properties, efficiency, and applicability of the present RKHS technique, five problems will be solved numerically in this chapter.

In this section, we have five nonlinear numerical examples that solved by using the RKHS method and the RK method of order 4, in order to show the accuracy and the ability of these methods for solving such systems. Here, we give the accuracy results especially for the RKHS method. After we obtained the current results or in other words the periodic solutions we compare them between the two presented algorithms. In the process of computation, all the symbolic and numerical computations are performed by using MATHEMATICA 9 software package.

**Example 3.1**

Consider the following nonlinear Hopfield neural network:
\[
\begin{align*}
x_1' &= -x_1 + 34tanh(x_1) - 1.6tanh(x_2) + 0.7tanh(x_3), \\
x_2' &= -x_2 + 2.5tanh(x_1) + 0.95tanh(x_3), \\
x_3' &= -x_3 - 3.5tanh(x_1) + 0.5tanh(x_2),
\end{align*}
\]
subject to initial conditions:
\[
\begin{align*}
x_1(0) &= -0.109, x_2(0) = -0.832, x_3(0) = 1.721,
\end{align*}
\]
where the period equal \( t \in [0, 250] \)
This is Hopfield neural network equation system with initial conditions that we need to use it in our algorithm to enable us get the results and the periodical solutions from zero to 250. Here, we selected this long period to enable the RKHS draw the results in utmost precision. Thus, and according to this accuracy result we can judge or decide how to act or behavior of the system. So, we will solve the equations for \( x_1, x_2, \) and \( x_3 \), then we will solve pairs of these equation by RKHS method. After applying the previous steps, we will repeat the same approach on the same system and initial condition but by using the RK method of order 4. Finally, we will compare the produced numerical solutions.

According to the numerical solutions in Figure 1 that produced by using the RKHS kernel method, we can conclude that these solutions are not chaotic, which means that, the form of the function behaviour was not chaotic. Anyhow, to make it chaotic system we added some values to be chaotic and this is existing in Example 3.3. So, in general the RKHS method gave solutions to...
this system and can solve it. In Figure 2, the numerical solutions are not chaotic also, and they take the same behavior of the solutions using the RKHS method. So, from these results we can conclude the solution between the RKHS and RK methods are agreement.

In Figure 3, we note in image (a) the result roughly equal and the same case in image (c). There is small difference in image (b) but also its agree with the other images so we can say that the RKHS able to solve the equations system of the Hopfield neural network in very efficiency and accuracy.

Example 3.2

Consider the following non-linear Hopfield Neural Network:

\[
\begin{align*}
x_1' &= -x_1 + 2\tanh(x_1) - 1.2\tan(x_2), \\
x_2' &= -x_2 + 2.5\tanh(x_1) + 1.71\tanh(x_2) + 1.15\tanh(x_3), \\
x_3' &= -x_3 - 4.75\tanh(x_1) + 1.1\tanh(x_3),
\end{align*}
\]

subject to initial conditions:

\[
\begin{align*}
x_1(0) &= -0.109, x_2(0) = -0.832, x_3(0) = 1.721,
\end{align*}
\]

where the period equal \( t \in [0, 250] \).

We solved this system by using the RKHS method and the RK method of order 4, to show the difference of the results between these two systems, and to show the performance of them to enable us decide which one the efficient method. After applying the two presented method, as in figure 4, we solved \( x_1(t), x_2(t), \) and \( x_3(t) \) equation each one alone by using the RKHS method, thats shown in images (a), (b), and (c) to compare these results with the results of the RK method of order 4 that will solve the same equations. We obtained the results thats appear in Figure 4.

In this second part of the example as shown in figure 5, we resolved this system by using the RK method of order 4. As a one time we resolved by it the equations with \( x_1 \) and the result was in image (a). In the second
step, we also resolved the equations \( x_1 \) with \( x_3 \) to obtain a chaotic periodical solution for these equations as in image (b), in image (c) we applied the RK method to solve equations \( x_2 \) with \( x_3 \) and the periodical solutions is also chaotic. Image (d) illustrates the group of solutions to the \( x_1, x_2 \) and \( x_3 \) which means we could have resolved each one separately by the RK method, but in this image we collected the three periodical results in one image to give chaotic form which means we are solving an chaotic Hopfield neural network equations system. In image (e) we showed you the result of solving equation \( x_1 \) by using the RKHS method and the RK method to display how each method solved this equation, and how was the performance of it, so we repeated this step also in equations \( x_2 \) and \( x_3 \). To compare between them by their results and their performance, and then decide if they can solve the Hopfield neural network equations system and in efficiently form. Virtually the results in image (e), (f), and (g) are approximately symmetric.

Fig. 5: The results of using RK4 method for the system in Example 3.2 and after obtained these results we compared them with the RKHS algorithm results for the same system.

Example 3.3

Making use of the solution of Example 3.2 as external inputs for Example 3.1, we set up the following Hopfield neural network:

\[
\begin{align*}
    x_1 &= -y_1 + 3.4tanh(x_1) - 1.6tanh(y_2) + 0.7tanh(y_3) + 0.0136tanh(y_3) - 0.0015tanh(x_2) + 0.0025tanh(x_3), \\
    x_2 &= -x_2 + 2.5tanh(x_1) + 0.5tanh(y_3) + 0.0005tanh(x_1) + 0.0212tanh(x_2) - 0.0005tanh(x_3), \\
    x_3 &= -x_3 - 3.5tanh(x_1) + 0.5tanh(x_2) + 0.0012tanh(x_3) + 0.0023tanh(x_2) + 0.015tanh(x_3),
\end{align*}
\]

subject to initial conditions:

\[
x_1 = -0.645, x_2 = 0.243, x_3 = -0.628,
\]

where the period equal \( t \in [0, 250] \). The following step we will solve the previous numerical Hopfield neural network system and calculate \( x_1, x_2, x_3 \) sequentially by using the RKHS method. The goal of these steps and computations to prove the ability of the RKHS method in solving the Hopfield neural network systems, and in efficiency form in addition to compare the numerical solutions of using RKHS method with the most famous mathematical method which means The Rang Kutta method of order 4, to show for the reader the results after the computations for the two methods are agreement. So after applying the RKHS as we see in figure 6 the previous results calculated by the RKHS method with a specific initial conditions and on the specific period that equal 250. For example in image (a) the equation \( x_1 \) have a chaotic periodical solution from \([0, 250]\) period, also the same case in \( x_2 \) and \( x_3 \) equations that shown in (b) and (c) images. Then we solved by the RKHS method the pairs of equation like \( x_1 \) and \( x_2, x_1 \) and \( x_3, x_2 \) and \( x_3 \), and they are shown in (e), (f), (g) images sequentially to watch their results that produced by the RKHS method then compare them with RK method in the same cases and the same pairs of the equations.
Example 3.4

Consider the following non-linear Hopfield Neural Network:

\[
\begin{align*}
    x_1' &= -x_1 + 2tanh(x_1) - tan(x_2), \\
    x_2' &= -x_2 + 1.7tanh(x_1) + 1.71tanh(x_2) + 1.1tanh(x_3), \\
    x_3' &= -x_3 - 4.75tanh(x_1) + 1.1tanh(x_2),
\end{align*}
\]

subject to initial conditions:

\[
x_1 = -0.109; x_2 = -0.832; x_3 = 1.721,
\]

where the period equal \( t \in [0, 250] \). As the previous approaches we will apply RKHS method on \( x_1, x_2 \) and \( x_3 \) to get the desired result and apply them also RK method to compare the current result and judge are they agreement or not. So we will begin with applying RKHS method on this numerical system firstly. See Figures 9 and 10.
Example 3.5

Consider the following non-linear Hopfield Neural Network [7]:

\[ x_1' = -x_1 + 3.4 \tanh(x_1) - 1.6 \tanh(x_2) + 0.7 \tanh(x_3) + 0.02 \tanh(x_1) + 0.035 \tanh(x_3), \]

\[ x_2' = -x_2 + 2.5 \tanh(x_1) + 0.95 \tanh(x_3) + 0.025 \tanh(x_2), \]

\[ x_3' = -x_3 - 3.5 \tanh(x_1) + 0.5 \tanh(x_2) + 0.004 \tanh(x_1) - 0.01 \tanh(x_2) + 0.05 \tanh(x_3), \]

subject to initial conditions:

\[ x_1(0) = -0.236, x_2(0) = 0.543, x_3(0) = -0.745, \]

where the period equal \( t \in [0, 250] \).

The following step we will solve the previous numerical system and calculate \( x_1, x_2 \) and \( x_3 \) by using reproducing kernel Hilbert space method then so we will find the numerical solutions to make sure of the reproducing kernel Hilbert space method able to solve this hop field neural network chaotic system. Let us begin solve this numerical system firstly by RKHS method then we will resolve it by RK method as we did in the previous examples but this time with different initial conditions. See Figures 11, 12 and 13.

4 Conclusions

We were able to prove that the RKHS method able to solve any numerical equations systems of the Hopfield neural network equations systems in accuracy and efficiency form according to the obtained results that we compared them with the numerical results which solved by using the other famous mathematical method RK method of order 4, and from this point we can decide or judge the numerical results that solved by these two methods are agreement so these agreement results encourage our invention. Finally, we can employ the reproducing kernel Hilbert space method in solving the Hopfield neural networks equations systems as we saw.
Fig. 11: As we saw, these numerical solutions are produced by applying the RKHS method in HNN equation system that the RKHS could solve and give accuracy solutions for one equation like $y_1$ or to the pairs of equations system like $x_1$ with $x_2, x_3$ with $x_3$ and $x_1$ with $x_3$. We can conclude as a final image the reproducing kernel Hilbert space has a good efficiency in solve HNN equation system.

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