

# A new particle filter based on organizational adjustment particle swarm optimization

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**Abstract:** A dynamic organizational adjustment particle swarm optimization-based particle filter algorithm (OAPSO-PF) is presented in this paper in order to solve the problem of low precision and complicated calculation of particle filter based on particle swarm optimization algorithm(PSO-PF). Through the mutual competition and collaboration among organizations, this algorithm allows the particles to adapt to the environment better and thus reach the goal of global optimization, accordingly enhancing the quality of particles and avoiding particle degradation by the adoption of optimal particle retention. Finally different models are used for simulation experiment and the results indicate that this new algorithm improves the operation speed and precision, it is applicable to practical engineering.

**Keywords:** particle filter; particle swarm optimization; organizational adjustment

## 1. Introduction

In the piratical engineering application, there is always flicker noise[1]. Flicker noise is characterized in distinct Gaussian feature, while most of the ordinary filter algorithms are within the framework of Kalman filter theory which will show relatively huge errors in system state and variance estimation giving large flicker noise, influencing the effect of radar tracking. Particle filter (PF) [2] is a statistic filtering based on Monte Carlo Method and Recursive Bayesian estimation. It is widely applied to positioning and navigation of non-Gaussian noise and non-linear system, fault diagnosis, target tracking and mode identification field [3] as its state function and observation function has no non-linear hypothesis. Nevertheless, PF may confront with the problem of weight degradation [4] which if solved by resampling method may result unavoidable particle impoverishment[5-6].

Particle swarm optimization-based PF (PSO-PF) is a typical representative of Intelligent Optimization Algorithm which introduces PSO algorithm into PF[7]. In PSO-PF, the sample distribution is inclined to move to the area with higher posterior probability [8]. PSO-PF improves the particle degradation of PF and is easier for actualization. Unfortunately PSO-PF is a process of iterative optimization

which will prolong the calculation time because of the high iterative frequency [9]. Moreover, PSO-PF may be easily trapped into local optimization, influencing the precision and stability of practical engineering application [10].

Proceeding from the perspective of organization, particles are used to form different organizations in this paper and X is put forward by fully making use of the individual collaboration feature and self-earning of organizations. A new particle filter algorithm based on dynamic organizational adjustment particle swarm optimization. The experimental results prove that OAPSO-PF improves the efficiency of particle filter.

## 2. Particle filter

Particle filter is an approximate calculation of Bayes estimation based on sampling theory. Combining Monte Carlo Method and Bayesian Theory together, particle filter follows the basic thought that to find a group of random sample for approximation of posterior probability density, replace the infinitesimal calculus in light of posterior probability density function by sample mean value, and thus acquire the minimal estimate of variance [11].

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Assuming the nonlinear dynamic process is expressed as follows:

$$x_k = f(x_{k-1}, v_{k-1}) \quad (1)$$

$$y_k = h(x_k, n_k) \quad (2)$$

If the initial probability density of the state is known as  $p(x_0|y_0) = p(x_0)$ , then the state predictive equation is:

$$p(x_k|y_{1:k-1}) = \int p(x_k|x_{k-1})p(x_{k-1}|y_{1:k-1})dx_{k-1} \quad (3)$$

and the state renewal equation is:

$$p(x_k|y_{1:k}) = \frac{p(y_k|x_k)p(x_k|y_{1:k-1})}{p(y_k|y_{1:k-1})} \quad (4)$$

Where

$$p(y_k|y_{1:k-1}) = \int p(y_k|x_k)p(x_k|y_{1:k-1})dx_k \quad (5)$$

Supposing there is a known and easily-sampling importance function  $q(x_{0:k}|y_{1:k})$ , which is rewrote as

$$q(x_{0:k}|y_{1:k}) = q(x_0) \prod_{j=1}^k q(x_j|x_{0:j-1}, y_{1:j}) \quad (6)$$

then the weight formula is

$$\begin{aligned} w_k &= \frac{p(y_{1:k}|x_{0:k})p(x_{0:k})}{q(x_k|x_{0:k-1}, y_{1:k})q(x_{0:k-1}, y_{1:k})} \\ &= w_{k-1} \frac{p(y_k|x_k)p(x_k|x_{k-1})}{q(x_k|x_{0:k-1}, y_{1:k})} \end{aligned} \quad (7)$$

To sample  $N$  sample points  $\{x_{k-1}^i\}_{i=1}^N$  from  $p(x_{k-1}|y_{1:k-1})$ , then the probability density is:

$$p(x_{k-1}|y_{1:k-1}) = \sum_{i=1}^N w_{k-1}^i \delta(x_{k-1} - x_{k-1}^i) \quad (8)$$

and the renewal probability density is:

$$w_k^i = w_{k-1}^i \frac{p(y_k|x_k^i)p(x_k^i|x_{k-1}^i)}{q(x_k^i|x_{k-1}^i, y_k)} \quad (9)$$

### 3. Algorithms in this paper

#### 3.1. principle of OAPSO

In economics, Coase[12] defined that "transaction cost" is for explanation of the size and formation of organization, Wilcox referring to Coase the method of reducing "transaction cost", two models are combined to bring forward the organization learning model [13], based on which the literature[14] comes up with the organization evolution algorithm. Being enlightened by this, this paper proceeds from the perspective of organization and put forward with

the organization adjustment particle swarm optimization which is then fused with particle filter.

In this article, individual is denoted by real-value vector, taking into account only the minimum, therefore the individual fitness  $F$  is defined as  $f(x)$ . Organization is the set of several individuals that are the members of the organization, wherein these individuals with the best fitness is the leader of the organization. If there is more than one member in an organization with the same optimal values, then the leader can be randomly selected from them. The fitness of the leader is that of the organization, and the intersection of different organizations is empty. Here are 4 types of organizational adjustment operators in the algorithm presented.

(1) Splitting operator. In this operator, the prerequisite for organization  $org$  splitting is as follows:

$$|org| > Max \quad (10)$$

where  $|org|$  denotes the number of member in  $org$ ,  $Max (< N_0)$  the allowable maximal number of organizational member,  $N_0$  the number of all organizational member in initialization,  $Max$  and  $N_0$  pre-set parameters. If a parent organization  $org_i$  meets the splitting prerequisite, then it will split into two progeny organizations  $org_{c1}$  and  $org_{c2}$  by the following method.  $|org_i|/3 \sim 2|org_i|/3$  members are selected randomly from  $org_i$  so as to form progeny organization  $org_{c1}$ , and the rest members from progeny organization  $org_{c2}$ . Then from the current population the organization  $org_i$  is deleted, while  $org_{c1}$  and  $org_{c2}$  are added to the next-generation evolutionary population.

(2) Annexation operator. Assuming two parent organizations of  $org_{i1} = \{x^1, x^2, \dots, x^{m1}\}$  and  $org_{i2} = \{y^1, y^2, \dots, y^{m2}\}$ ,  $m_1$  and  $m_2$  are the number of members in organization  $org_{i1}$  and  $org_{i2}$ , and  $Fitness(org_{i1}) \geq Fitness(org_{i2})$ , then a self-attached organization  $org_c = \{z^1, z^2, \dots, z^{m1+m2}\}$  can be generated by annexing  $org_{i2}$  through  $org_{i1}$ , wherein  $z^i = x^i, i = 1, 2, \dots, m_1$ . If  $U_{j+m1}(0, 1) < AS$ ,  $z^{j+m1}$  ( $j = 1, 2, \dots, m_2$ ), then it will be generated by annexation strategy 1, or otherwise by annexation strategy 2. Here the subscript in  $U_{j+m1}(0, 1)$  denotes each random number generated by  $j + m_1$ ,  $AS \in (0, 1)$  is a pre-set parameter. Two annexation strategies are presented as follows.

Assuming the leader of  $org_{i1}$  is  $(a_1, a_2, \dots, a_n)$ , and the new individual is  $r_j = (r_{j,1}, r_{j,2}, \dots, r_{j,n}), j = 1, 2, \dots, m_2$ . Then in annexation strategy 1,  $r_j$  is generated by the following equation:

$$r_{j,k} = \begin{cases} x_k, & d_{j,k} < x_k \\ \bar{x}_k, & d_{j,k} > x_k \\ d_{j,k}, & \text{otherwise} \end{cases} \quad (11)$$

in which,  $d_{j,k} = a_k + U_k(0, 1) \times (a_k - y_k^j), k = 1, 2, \dots, n$ . In annexation strategy 1,  $r_j$  is generated by the following equation:

$$r_{j,k} = \begin{cases} x_k + \beta_k \times (\bar{x}_k - x_k), & U_k(0, 1) < 1/n \\ a_k, & \text{otherwise} \end{cases} \quad (12)$$

where  $k = 1, 2, \dots, n$ ,  $\beta_k = U(0, 1)$ . After  $r_j$  is calculated, it is further verified by the following equation  $z^{j+m1}$ :

$$z^{j+m1} = \begin{cases} r_j, & \text{Fitness}(r_j) \geq \text{Fitness}(y^j) \\ r_j, & \text{Fitness}(r_j) \geq \text{Fitness}(y^j) \text{ and } \{U_j(0, 1) < \exp(\text{Fitness}(r_j) - \text{Fitness}(y^j))\} \\ y^j, & \text{otherwise} \end{cases} \quad (13)$$

In fact, annexation strategy 1 is a heuristic crossover operator, while annexation strategy 2 is mutation operator. From equation (13), it can be observed that when the fitness of  $r_j$  exceeds  $y^j$ ,  $r_j$  enters *org<sub>c</sub>* for enhancement of organization fitness; when the fitness of  $r_j$  is better than  $y^j$ ,  $r_j$  may enter *org<sub>c</sub>* at some probability, that is, the closer the fitness of  $r_j$  to  $y^j$ , the larger the probability will be, and this conduces to protection of population diversity. Finally, *org<sub>i1</sub>* and *org<sub>i2</sub>* are deleted from the population, and *org<sub>c</sub>* is added to the next-generation population.

(3) Cooperation operator. Given two parent organizations of *org<sub>i1</sub>* = { $x^1, x^2, \dots, x^{m1}$ } and *org<sub>i2</sub>* = { $y^1, y^2, \dots, y^{m2}$ }, if  $U(0, 1) < CS$ , then the two progeny organizations *org<sub>c1</sub>* and *org<sub>c2</sub>* will be generated by cooperation strategy 1, or otherwise by strategy 2. Here  $CS \in (0, 1)$  is a pre-set parameter, and the two cooperation strategies are as follows:

Let  $(a_1, a_2, \dots, a_n)$  be the leader of *org<sub>i1</sub>*,  $(b_1, b_2, \dots, b_n)$  the leader of *org<sub>i2</sub>*, and two new individuals generated from cooperation  $u = (u_1, u_2, \dots, u_n)$  and  $l = (l_1, l_2, \dots, l_n)$ , then in cooperation strategy 1,  $u$  and  $l$  can be generated by the following equation:

$$\begin{cases} u_k = \beta_k \times a_k + (1 - \beta_k) \times b_k \\ l_k = (1 - \beta_k) \times a_k + \beta_k \times b_k \end{cases} \quad (14)$$

where,  $k = 1, 2, \dots, n$ ,  $\beta = U(0, 1)$ .

In cooperation strategy 2,  $u$  and  $l$  are generated by

$$\begin{cases} u = (a_1, a_2, \dots, a_{i-1}, b_{i+1}, \dots, b_{i2}, a_{i2+1}, a_{i2+2}, \dots, a_n) \\ l = (b_1, b_2, \dots, b_{i-1}, a_{i+1}, \dots, a_{i2}, b_{i2+1}, b_{i2+2}, \dots, b_n) \end{cases} \quad (15)$$

after  $u$  and  $l$  generated, *org<sub>c1</sub>* and *org<sub>c2</sub>* are respectively confirmed as:

$$org_{c1} = \begin{cases} \{x^1, x^2, \dots, x^{i-1}, u, x^{i+1}, \dots, x^{m1}\}, \\ \exists x_i \in org_{i1}, \text{Fitness}(x^i) < \text{Fitness}(u) \\ org_{i1}, & \text{otherwise} \end{cases} \quad (16)$$

$$org_{c2} = \begin{cases} \{y^1, y^2, \dots, y^{j-1}, l, y^{j+1}, \dots, y^{m2}\}, \\ \exists y_i \in org_{i2}, \text{Fitness}(y^j) < \text{Fitness}(l) \\ org_{i2}, & \text{otherwise} \end{cases} \quad (17)$$

Finally *org<sub>i1</sub>* and *org<sub>i2</sub>* can be deleted from the current population, and *org<sub>c1</sub>* and *org<sub>c2</sub>* are added to the next-generation population. In fact, Cooperation Strategy 1 is arithmetic crossover, and Strategy 2 is discrete crossover.

(4) Speed update operator. Let  $h^g(t) = (h_1^g, h_2^g, \dots, h_n^g)^T$  denote the position experienced by the optimal leader in all

organizations,  $h^i(t) = (h_1^i, h_2^i, \dots, h_n^i)^T$  denotes the best position experienced by the leaders in *i*th organization. Then particles in *i*th organization update their speeds and positions in *t*th generation by the following approach:

$$\begin{cases} v_j^i(t+1) = w(t)v_j^i(t) + c_1r_1(h_1^i(t) - x_j^i(t)) + c_2r_2(h_j^g(t) - x_j^i(t)) \\ x_j^i(t+1) = x_j^i(t) + v_j^i(t+1) \end{cases} \quad (18)$$

Here inertia weight is employed in order to update the speed and position vectors. When the inertia weight is relatively large, the algorithm is capable of exploring a greater searching space. In the final stage, the smaller inertia weight will perform delicate detection of the searching space.

### 3.2. analysis on convergence of OAPSO

If an individual component  $x^i$  is denoted by  $L$  bit binary string, then it means to quantify the interval  $[x, \bar{x}]$  into  $2^L$  discrete values and precision is  $\varepsilon = (\bar{x} - x)/2^L$ , so the convergence of the algorithm can be directly analyzed by real coding. Given the required precision  $\varepsilon$ , then the searching space  $S$  can be regarded as discrete space with the size as follows:

$$|S| = \prod_{i=1}^n \left[ \frac{\bar{x}_i - x_i}{\varepsilon} \right] \quad (19)$$

For each element  $x \in S$ , its fitness is  $Fitness(x)$ . Let  $F = \{Fitness(x) | x \in S\}$ , apparently  $|F| \leq |S|$ , which is equivalent to  $F = \{F_1, F_2, \dots, F_{|F|}\}$  where  $F_1 > F_2 > \dots > F_{|F|}$ . Based on different  $Fitness(x)$ ,  $S$  can be classified into several nonvoid subset  $\{S_i\}$ , in which  $S_i = \{x | x \in S \text{ and } Fitness(x) = F_i\}$ ,  $i = 1, 2, \dots, |F|$ , then

$$\bigcup_{i=1}^{|F|} S_i = S \quad (20)$$

$$\sum_{i=1}^{|F|} |S_i| = |S| \quad (21)$$

$$S_i \cap S_j = \emptyset, \forall i \neq j \quad (22)$$

$$S_i \neq \emptyset, \forall i \in \{1, 2, \dots, |F|\} \quad (23)$$

$F_1$  is the global optimal solution  $F^*$ , whereas the set  $S_1$  contains all individuals whose fitness equals to  $F^*$ .

In this algorithm, the number of organization varies with the frequency of adjustment, while the total number of individuals remains the same, e.g., the population  $q = \{x^1, x^2, \dots, x^{N0}\}$ . Let  $Q$  denote the set of all populations, then the number of such populations is:

$$|Q| = \binom{S + N_0 - 1}{N_0} \quad (24)$$

To measure the strengths and weaknesses of such population, the fitness of  $q$  is defined as:

$$Fitness(q) = \max\{Fitness(x^i) | i = 1, 2, \dots, N_0\} \quad (25)$$

therefore  $F_{|F|} \leq Fitness(q) \leq F_1, \forall q \in Q$ .

$Q$  is divided into nonvoid subset  $\{Q_i\}$

$$Q_i = \{q | q \in Q \text{ and } Fitness(q) = F_i\}, \quad (26)$$

$$i = 1, 2, \dots, |F|$$

Obviously,

$$\bigcup_{i=1}^{|F|} Q_i = Q \quad (27)$$

$$Q_i \neq \emptyset, \forall i \in \{1, 2, \dots, |F|\} \quad (28)$$

and set  $Q_i$  contains all populations with fitness.

Let  $q_{ij}$  denotes the  $j$ th population in  $Q_i, i = 1, 2, \dots, |F|, j = 1, 2, \dots, |Q|$ . With the function of organization evolution operator, population state transfer from  $q_{ij}$  to  $q_{kl}$  can be expressed as  $q_{ij} \rightarrow q_{kl}$ . Let  $pr_{ij,kl}$  the probability of  $q_{ij}$  transferring to  $q_{kl}$ ,  $pr_{ij,k}$  the probability of  $q_{ij}$  transferring to any of the population in  $Q_k$ , and  $pr_{i,k}$  the probability of any population in  $Q_i$  transferring to any of the population in  $Q_k$ , then apparently

$$pr_{ij,k} = \sum_{l=1}^{|Q_k|} pr_{ij,kl}, \sum_{k=1}^{|F|} pr_{ij,k} = 1, pr_{i,k} \geq pr_{ij,k} \quad (29)$$

The global convergence of this optimization method is proved below:

**Definition1.** An evolutionary algorithm converges to the global optimum solution, iff

$$\lim_{t \rightarrow \infty} pr\{Fitness(q(t)) = F^*\} = 1 \quad (30)$$

where  $pr$  denotes probability,  $q(t)$  the  $t$ th generation population.

**Theorem 1.** When the organization adjust the particle swarm,  $\forall i, k \in \{1, 2, \dots, |F|\}$ , then

$$\begin{cases} pr_{i,k} > 0, & k \leq i \\ pr_{i,k} = 0, & k > i \end{cases} \quad (31)$$

**Demonstration:**  $\forall q_{ij} \in Q_i \Rightarrow \exists x^l \in q_{ij}, Fitness(x^l) = F_i, j = 1, 2, \dots, |Q_i|$ . Given the population  $q_{ij}$  transferred to  $q_{kl}$  under the function of organization evolutionary operator. Splitting operator does not generate any new individuals, but just transfers some particles to another organization, so it does not take any impact on the population fitness. Besides, in the annexation and cooperation operators, the parent leaders with greater adaptability in two parental organizations are duplicated to the progeny organizations. Finally, in the speed update operator, particles are moving toward the current optimal value with a specific weight. Since the retaining of optimal individual is used in the process of speed update operator, if the particles after speed update precedes the current optimal individual, then the new particles will be replaced by the current-generation particles; otherwise the current-generation particles should

be retained. Because  $x^l$  is definitely a leader in population  $q_{ij}$  with fitness no less than other leaders, then

$$x^l \in q_{kl} \Rightarrow Fitness(q_{kl}) \geq Fitness(q_{ij}) \Rightarrow k \leq i$$

$$\Rightarrow pr_{i,k} = 0, \forall k > i \quad (32)$$

Given individual  $x^l$  with  $Fitness(x^l) = F_k, k \leq i$  and  $x^l$  has  $n_1$  components  $\{x_1, x_2, \dots, x_{n_1}\}$ , wherein each component is different from those corresponding to the positions by  $x^l$ .  $\exists org \in q_{ij}$  and the leader of  $org$  is  $leader = x^l$ . Supposing  $|org| \leq Max$ , then the probability of executing annexation operator on  $org$  is  $pr_1 = (1 - |org|/N_0)/2 > 0$ . In annexation operator strategy 2, for each component, if  $U(0, 1) < 1/n$ , then the component will be randomly re-elected from  $[\bar{x}_i, x_i]$ , thus the probability of generating  $x^l$  by  $x^l$  is

$$pr_2 = (1 - \frac{1}{n})^{(n-n_1)} \cdot \prod_{i=1}^{n_1} \frac{\epsilon}{n(\bar{x}_i - x_i)} > 0 \quad (33)$$

After the effect of evolutionary operator, the probability of transferring from  $q_{ij}$  to any population in  $Q_k$  is

$$pr_{ij} > pr_1 \times (1 - AS) \times pr_2 > 0 \quad (34)$$

Therefore,  $pr_{i,k} \geq pr_{ij,k} > 0, \forall k \leq i$ .

**Theorems2.** Organizational evolutionary algorithm feature global convergence.

**Demonstration:** Elitism strategy is employed here. From Theorem 1,  $pr_{i,k} > 0, k \leq i$  can be inferred that the probability transferring from one state to another  $pr > 0$ , e.g., Hence the probability of failure in finding the optimal solution for the probability is

$$\lim_{n \rightarrow \infty} (1 - c)^n = 0 \quad (35)$$

In other words, this optimized algorithm finds the optimal solution with probability 1, and thus features global convergence.

### 3.3. process of OAPSO-PF

(1) When  $k=0$ , take  $N$  particles as samples from importance function at the initial time. The fitness function are expressed in equation(36)

$$Fitness = \exp\left[-\frac{1}{2R_k} (z_{New} - z_{Pred})\right] \quad (36)$$

Meanwhile, Assume these  $N$  samples as  $N$  initial organizations.

(2) calculate the importance value:

$$w_k^i = w_{k-1}^i p(z_k | x_{k-1}^i) = w_{k-1}^i p(z_k | x_k^i) \quad (37)$$

(3) if the termination conditions are satisfied, go to step (6), Otherwise execute the next step.

(4) If each organization meets the splitting condition, then execute the splitting operator.

(5) Randomly select two parental organization  $org_{i1}$  and  $org_{i2}$ , then randomly select annexation or cooperation operators that are applied to the two parental organization.

(6) Update the speed and position of particles, calculate the speed  $v_k^{im}$  of particle  $x_k^{im}$  after  $m$ th iteration through equation (38). By using equation (39), the particle  $x_k^{im}$ , under the effect of speed  $v_k^{im+1}$ , reach the position  $x_k^{im+1}$  of next iteration:

$$v_k^{im+1}(t+1) = w(t)v_k^{im+1}(t) + c_1r_1(pb_{k-1}^i - x_k^{im}) + c_2r_2(pg_k - x_k^{im}) \quad (38)$$

$$x_{k+1}^{im+1} = x_k^{im} + v_k^{im+1} \quad (39)$$

(7) Compare their fitness, update  $pb$  and  $pg$ :

$$pb_k^i = \begin{cases} pb_k^i, & Fitness(x_g) < Fitness(pb_k^i) \\ x_g, & Fitness(x_g) > Fitness(pb_k^i) \end{cases} \quad (40)$$

$$pg_k \in \{x_k^1, x_k^2, x_k^3, \dots, x_k^N | Fitness(x)\} \\ = \max\{Fitness(x_k^1), Fitness(x_k^2), \dots, Fitness(x_k^N)\} \quad (41)$$

(8) When the optimal value of particle complies with the initially-set threshold value  $\epsilon$  or algorithm reached maximum iteration times  $\lambda$ , optimization should be stopped. Else jump to step(3).

(9) Calculate the importance weight of the particles after optimization and perform normalization:

$$w_k^i = w_k^i / \sum_{i=1}^N w_k^i \quad (42)$$

(10) State output:

$$\tilde{x} = \sum_{i=1}^N w_k^i x_k^i \quad (43)$$

## 4. Simulation experiment

### 4.1. Univariate nonstationary growth model

Choosing a univariate nonstationary growth model (UNGM) [15], let  $w(t)$  and  $v(t)$  are zero-mean Gaussian noise, the process and measurement model of the simulated objects are given as follows:

$$x(t) = 0.5x(t-1) + \frac{25x(t-1)}{1 + [x(t-1)]^2} + 8\cos[1.2(t-1)] + w(t) \quad (44)$$

$$z(t) = \frac{x(t)^2}{20} + v(t) \quad (45)$$

By using three algorithm, state estimation and tracking of this non-linear system are performed.

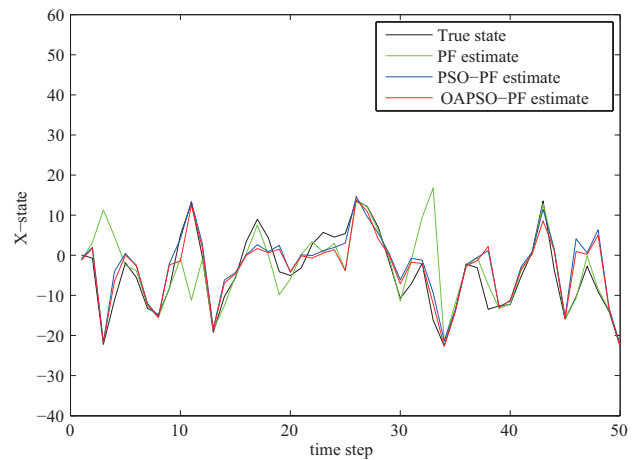


Figure 1 state estimation of different algorithm

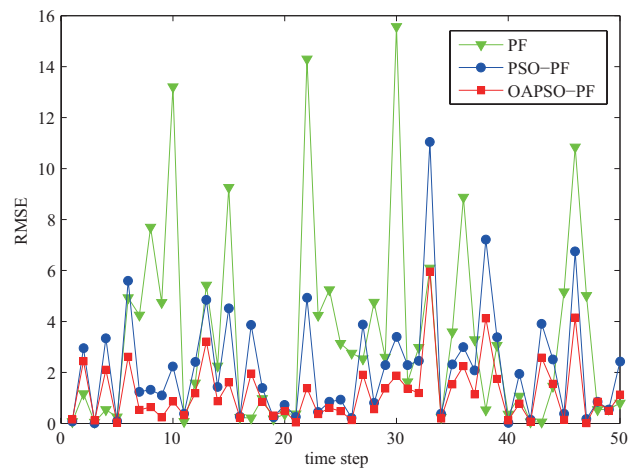
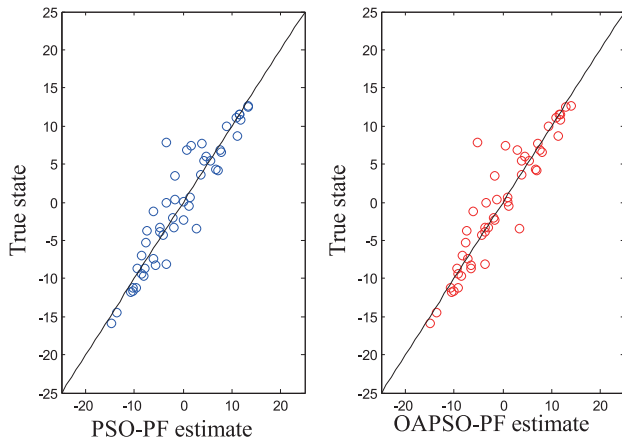


Figure 2 RMSE of different algorithm

Table 1 comparison of simulation by UNGM model in different parameters environment ( $Q = 10$ )

Parameters	Algorithm	RMSE	Time
$\epsilon = 0.05 \lambda = 100$	PSO-PF	1.9625	0.3672
	OAPSO-PF	1.3728	0.3387
$\epsilon = 0.05 \lambda = 200$	PSO-PF	1.7637	0.5303
	OAPSO-PF	1.3201	0.3809
$\epsilon = 0.075 \lambda = 100$	PSO-PF	1.678	0.5136
	OAPSO-PF	1.170	0.4885
$\epsilon = 0.075 \lambda = 200$	PSO-PF	1.4942	0.7054
	OAPSO-PF	1.0852	0.5963

Giving the process noise variance  $Q = 10$ , measurement noise variance  $R = 1$ , and particle number  $N = 100$ , and initially-set threshold value  $\epsilon$  and maximum iteration times is  $\lambda$ , simulation is conducted.



**Figure 3** comparison of correlation

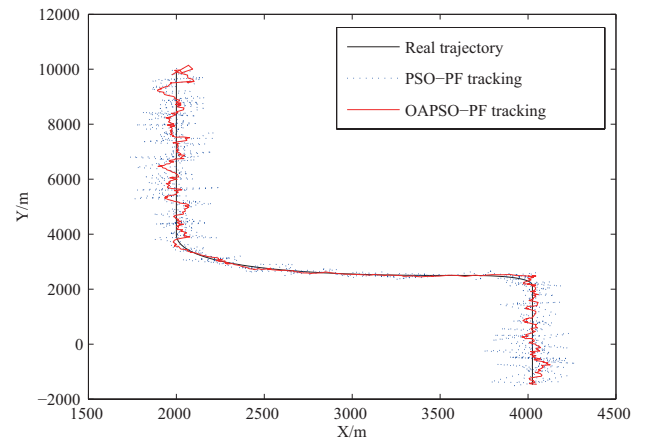
From the experimental result, it is apparent that giving different noise intensities, the errors of PSO and OAPSO-PF are obviously lower than the standard PF as the particle swarm optimization is an iterative optimizing process, which effectively increases the effectiveness of particles. OAPSO-PF can achieve the best precision, correlation, and reduces calculation time compared to PSO-PF. In addition, it can be observed from Table 1 that the change of maximum number of iteration will influence greatly the changes of OAPSO-PF, which also indicates that OAPSO-PF increases the success of optimization and reduces the probability of reaching the maximum iterations.

### 4.2. target tracking model

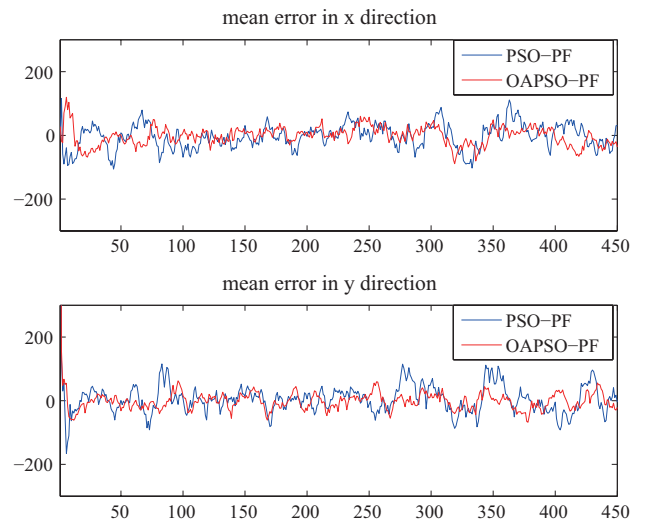
Given that the radar is tracking a target moving on a flat surface and in uniform linear motion along y axis at  $t = 0 \rightarrow 400$ th second, during which the speed is  $-15m/s$  and the starting point of target is (2000m, 1000m). At  $t = 400 \rightarrow 600$  the target turns slowly at  $90^\circ$  along x axis, wherein the accelerated speed is  $u_x = u_y = 0.075m/s^2$  and the speed decreases to 0 after the turning. The slow turning since  $t = 610s$  at  $90^\circ$  showed accelerated speed  $u_x = u_y = 0.3m/s^2$ , and ended at 660s where the accelerated speed decreased to 0. The radar scanning cycle is  $T = 2s$ .

**Table 2** comparison of simulation parameters

Algorithm	Absolute value of error in X direction	Absolute value of error in Y direction	Time
PSO-PF	32.7382	49.6251	4.6572
OAPSO-PF	24.7261	35.4621	4.2108



**Figure 4** different algorithm's performance in tracking



**Figure 5** mean curve of filter error

The simulation results show that errors in target tracking at the turning are increasing, while PSO-PF displays more evident errors. The tracking trace fluctuates a lot, while the error of OAPSO-PF is smaller. At the same time, a better tracking trace fitness and a shorter calculation time are proved, conducting to accurate and high-efficient tracking of maneuvering target turning continuously.

## 5. Conclusion

Standard PSO-PF only uses the memory feature of particles in particle swarm optimization, whereas other features are neglected. The algorithm presented here makes full use of coordination and self-learning features of the individuals in an organization to guide the particles to evolve con-

stantly, finally reaching the goal of global optimization. At last through experiment the performance of the algorithm is analyzed and the results may suggest that this algorithm features stable performance and high successful rate, accordingly helping to enhance the efficiency of particle filtering.

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