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On Analytical Prognosis Of Epitaxial Grows From Gas Phase. A Possibility To Improve Properties Of Films

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Abstract: In this paper we introduce an analytical approach to calculate the distribution of velocity of flow of the gas mixture, the concentration distributions of the growth component and temperature fields in the zone of deposition of semiconductor layers in chemical vapor deposition using a reaction chamber with a rotating disk substrate holder. The results of analysis of the temperature and concentration fields in the reduced and atmospheric conditions (~ 0.1 atm.) pressure in the reaction chamber obtained based on the proposed theoretical models and have good agreement with experimental data. Results of analytical modelling have been compared with experimental data.

Keywords: Gas phase epitaxy; Analytical approach for prognosis; Recommendations to improve properties of epitaxial layers.

high-frequency heater of graphite keeper of substrate. A flow of mixture of gases coming into the considered reaction chamber. Several components of the mixture of

1 Introduction

At the present time one of main technological processes of manufacturing of devices of micro- and nanoelectronics is manufacturing semiconductor layers by epitaxy from gas phase and molecular beams [1-5]. Methods of grown are intensively improving. At the same time modeling of physical processes that occur during the growth of epitaxial layers is weakly elaborated. In this situation relations between technological parameters, which determine kinetic and mechanisms of growth of epitaxial layers, could leads to essential errors. Main aim of the present paper is development of methods of modeling of several physical processes, which are existing during epitaxy from gas phase in a reaction chamber with rotating disk keeper of substrate (see Fig. 1).

Similar technological scheme is main scheme for epitaxy from gas phase with using organo- metallic compounds (MOC) and hydrides as initial materials (MOCVD) framework one of perspective approaches of manufacturing of semiconductor nanoheterostructures [2,3]. The considered in Fig. 1 reactor includes into itself

gases, which chemically reacting in the considered chamber during growth of an epitaxial layer. Another component of the considered mixture of gases is hydrogen, which is considered as gas-carrier.

2 Method of Analysis

To model physical processes, which are existing during growth epitaxial growth, we assume, that vector of linear speed of vector linear velocity entering the reaction chamber the flow perpendicular to the surface of the substrate holder disc keeper of substrate, which rotates with angular velocity ω . In this paper we analyzed flow of the mixture of gases at atmosphere pressure and at low pressure (\sim 0,1 of atmosphere pressure) in reaction chamber, distribution of temperature and distribution of concentration of growth component in growth zone of epitaxial layer.

We determine required values by solving the second



Fick's and Fourier laws for convective diffusion and the Navier-Stokes equation. We calculate distribution of considered concentration at the distance from the surface of disk of keeper of substrate with radius R, which approximately equal to thickness of diffusion layer [3]. We determine spatio-temporal distribution of temperature

viscosity. We consider regime of limiting flow of diffusion mass transport of growth component. In this limiting case we assume, that all particles of growth component precipitating and ordering on the substrate. We also assume, that flow is homogenous and one dimension in the inlet of reaction zone. In this situation boundary and initial

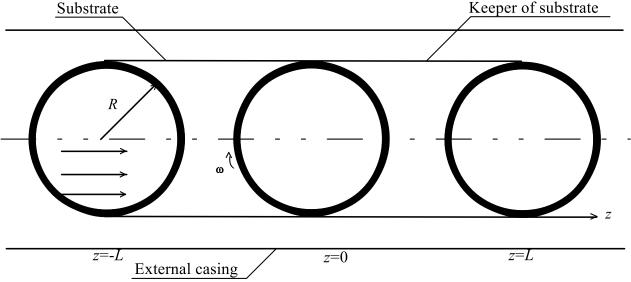


Fig 1. Schematic representation of reaction chamber for gas phase epitaxy

$$c(T)\frac{\partial T}{\partial t} = p + div[\lambda \cdot grad(T) - \mathbf{v} \cdot c(T) \cdot T \cdot C]^{(1)}$$

by solution the following heat equation [6] where υ is the speed of mixture of gases; c (T) is the heat capacitance; T (r,ϕ,z,t) is the spatio- temporal distribution of temperature; p is the density of power, which exudes in the system keeper of substrate - substrate; C (r,ϕ,z,t) is the spatio-temporal distribution of concentration of growth component, which was generated during chemical reaction. During solution of the Eq.(1) it is necessary to take into account flowing of gas and appropriate distribution of concentration of growth component. We determine the required values by joint solution of the Navier-Stokes equation and the second Fourier law with convective term. The equations could be written as

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\nabla \left(\frac{P}{\rho}\right) + \nu \Delta \mathbf{v}$$
 (2)

$$\frac{\partial C}{\partial t} = div \left[D \cdot grad C - \mathbf{v} \cdot C \right] \tag{3}$$

Here D is the diffusion component of growth component; P is the pressure; ρ is the density; ν is the kinematic

conditions could be written as

$$\begin{aligned} & (r, \varphi, z, 0) = C_0 \delta(z + L), C(0, \varphi, z, t) \neq \infty, \\ & \frac{\partial C(r, \varphi, z, t)}{\partial r} \bigg|_{r = R} = 0, \\ & \frac{\partial C(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 0} = \frac{\partial C(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 2\pi}, \\ & -\lambda \frac{\partial T(r, \varphi, z, t)}{\partial r} \bigg|_{\varphi = 0} = \frac{\partial T(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 2\pi}, \\ & \frac{\partial T(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 0} = \frac{\partial T(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 2\pi}, \\ & -\lambda \frac{\partial T(r, \varphi, z, t)}{\partial z} \bigg|_{z = -L} = \sigma T^4(r, \varphi, -L, t), T \\ & \frac{\partial C(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 0} = \frac{\partial C(r, \varphi, z, t)}{\partial \varphi} \bigg|_{\varphi = 2\pi}, \end{aligned}$$

 $C(r,\varphi,-L,t) = C_0$, $C(r,\varphi,0,t) = 0$, $C(r,0,z,t) = C(r,2\pi,z,t)$, $C(r,\varphi,-L,t) = C(r,2\pi,z,t)$



(5f)

$$\frac{\partial v_r(r,\varphi,z,t)}{\partial r}\bigg|_{r=0} = \frac{\partial v_r(r,\varphi,z,t)}{\partial r}\bigg|_{r=R},$$

$$\frac{\partial v_{\varphi}(r,\varphi,z,t)}{\partial \varphi}\bigg|_{\varphi=0} = \frac{\partial v_{\varphi}(r,\varphi,z,t)}{\partial \varphi}\bigg|_{\varphi=2\pi}$$

$$-\lambda \frac{\partial T(r,\varphi,z,t)}{\partial z}\bigg|_{z=L} = \sigma T^4(r,\varphi,z,t).$$

$$T (0, \varphi, z, t) \neq \infty, vr(r, \varphi, -L, t) = 0, vr(r, \varphi, 0, t) = 0,$$

$$\tag{4}$$

 $v_r(r, \varphi, L, t) = 0$, $T(r, \varphi, z, 0) = T_r$, $v_r(r, 0, z, t) = v_r(r, 2\pi, z, t)$, $v_r(0, \varphi, z, t) \neq \infty$, $v_{\varphi}(r, \varphi, 0, t) = \omega r$,

 $v_{\varphi}\left(r,\varphi,-L,t\right)=0,\ v_{\varphi}\left(r,\varphi,L,t\right)=0,\ v_{\varphi}(r,0,z,t)=v_{\varphi}(r,2\pi,z,t),\ v_{\varphi}(0,\varphi,z,t)\neq\infty,\ v_{z}(r,\varphi,-L,t)=V_{0},$

 $v_z(r, \varphi, 0, t) = V_0$, $v_z(r, \varphi, L, t) = 0$, $v_z(r, 0, z, t) = v_z(r, 2\pi, z, t)$, $v_z(0, \varphi, z, t) \neq \infty$, $v_z(r, \varphi, z, 0) = 0$,

$$v_{\varphi}(r, \varphi, z, 0) = 0, v_{z}(r, \varphi, -L, 0) = V_{0}$$

Here σ is the Stefan-Boltzmann constant; Tr is the temperature of cooled by water walls of reaction chamber; $\upsilon 0$ is the linear speed of gas flow in inlet area of growth zone; r, φ , z and t are the cylindrical coordinates and time; C0 is the concentration of growth component in flow of gas mixture in inlet area of area of growth of layers; S is the surface of keeper of substrate with substrate.

Equations for components of speed of gas flow by using cylindrical coordinates could be written as

$$\frac{\partial v_{r}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{r}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{r}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{r}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{r}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{\partial}{\partial r} \left(\frac{P}{\rho} \right)$$
(5a)
$$\frac{\partial v_{r}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{\varphi}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{\varphi}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{\varphi}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{r}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{1}{r} \frac{\partial}{\partial \varphi} \left(\frac{P}{\rho} \right)$$
(5b)
$$\frac{\partial v_{z}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{z}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{z}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{z}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{r}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{\partial}{\partial z} \left(\frac{P}{\rho} \right)$$
(5c)

We assume, that gas in the considered reaction chamber is ideal. In this situation the following equation is correct

$$P = \rho RT/M. \tag{6}$$

$$\frac{\partial v_r}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_r}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v_r}{\partial \varphi^2} + \frac{\partial^2 v_r}{\partial z^2} \right] - v_r \frac{\partial v_r}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_z \frac{\partial v_z}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial r} \tag{5d}$$

$$\frac{\partial v_r}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{\varphi}}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v_{\varphi}}{\partial \varphi^2} + \frac{\partial^2 v_{\varphi}}{\partial z^2} \right] - v_r \frac{\partial v_r}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_z \frac{\partial v_z}{\partial z} - \frac{R}{rM} \frac{\partial T}{\partial \varphi} \tag{5e}$$

$$\frac{\partial v_z}{\partial z} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_z}{\partial z} \right) + \frac{1}{r^2} \frac{\partial^2 v_z}{\partial \varphi^2} + \frac{\partial^2 v_z}{\partial z} \right] - v_r \frac{\partial v_r}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_z \frac{\partial v_z}{\partial z} - \frac{R}{rM} \frac{\partial T}{\partial \varphi} \tag{5e}$$

We calculate solution of the above system of equations by method of averaging of function corrections [7-11]. Framework the approach to determine the first-order approximations of components of flow of mixture of gases we replace the components on not yet known their average values $v_r \rightarrow \alpha_{1r}$, $v_{\varphi} \rightarrow \alpha_{1\varphi}$, $v_z \rightarrow \alpha_{1z}$ in right sides of Eqs. (5). The replacement leads to transformation of the Eqs.(5*d*)-(5*f*) to the following form

$$\frac{\partial v_{1r}}{\partial t} = -\frac{R}{M} \frac{\partial T}{\partial r}, \qquad \frac{\partial v_{1\varphi}}{\partial t} = -\frac{R}{M} \frac{\partial T}{\partial \varphi},
\frac{\partial v_{1z}}{\partial t} = -\frac{R}{M} \frac{\partial T}{\partial z}. \tag{7}$$

Solutions of the Eqs.(7) could be written as

$$\upsilon_{1r} = -\frac{R}{M} \frac{\partial}{\partial r} \int_{0}^{t} T \, d\tau \cdot \upsilon_{1\varphi} = -\frac{R}{M \, r} \frac{\partial}{\partial \varphi} \int_{0}^{t} T \, d\tau,$$

$$\upsilon_{1z} = -\frac{R}{M} \frac{\partial}{\partial z} \int_{0}^{t} T \, d\tau \, \cdot \tag{8}$$

The second-order approximations of components of speed of flow of mixture of gases could be obtained by replacement of the components in right sides of Eqs. (5) on the following sums: $\upsilon r \rightarrow \alpha 2r + \upsilon 1r$, $\upsilon \phi \rightarrow \alpha 2\phi + \upsilon 1\phi$, $\upsilon z \rightarrow \alpha 2z + \upsilon 1z$. Equations for the second-order approximations could be written as

$$\frac{\partial v_{2r}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{1r}}{\partial r} \right) + \frac{1}{r^2} \frac{\partial^2 v_{1r}}{\partial \varphi^2} + \frac{\partial^2 v_{1r}}{\partial z^2} \right] - (\alpha_{2r} + v_{1r}) \frac{\partial v_{1r}}{\partial r} - \frac{(\alpha_{2\varphi} + v_{1\varphi})}{r} \frac{\partial v_{1\varphi}}{\partial \varphi} - (\alpha_{2z} + v_{1z}) \frac{\partial v_{1z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial r}$$

(8a)

$$\frac{\partial v_{r}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{r}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{r}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{r}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{r}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial r}$$

$$(5d) \qquad (5d) \qquad -\left(\alpha_{2r} + v_{1r}\right) \frac{\partial v_{1r}}{\partial r} - \frac{\left(\alpha_{2\varphi} + v_{1\varphi}\right)}{r} \frac{\partial v_{1\varphi}}{\partial \varphi} - \left(\alpha_{2z} + v_{1z}\right) \frac{\partial v_{1z}}{\partial z} - \frac{R}{r} \frac{\partial T}{\partial \varphi}$$

(8b)

$$\frac{\partial v_{z}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{z}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{z}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{z}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{r}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial z} \qquad \qquad \frac{\partial v_{2z}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{1z}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{1z}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{1z}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{z}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial z} \qquad \qquad \frac{\partial v_{2z}}{\partial t} = v \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial v_{1z}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} v_{1z}}{\partial \varphi^{2}} + \frac{\partial^{2} v_{1z}}{\partial z^{2}} \right] - v_{r} \frac{\partial v_{z}}{\partial r} - \frac{v_{\varphi}}{r} \frac{\partial v_{\varphi}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial \varphi} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial z} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial z} - v_{z} \frac{\partial v_{z}}{\partial z} - \frac{R}{M} \frac{\partial T}{\partial z} - v_{z} \frac{\partial v_{z}}{\partial z} - v_{z} \frac{\partial v_{z$$



$$-\left(\alpha_{2r}+v_{1r}\right)\frac{\partial v_{1r}}{\partial r}-\frac{\left(\alpha_{2\varphi}+v_{1\varphi}\right)}{r}\frac{\partial v_{1\varphi}}{\partial \varphi}-\left(\alpha_{2z}+v_{1z}\right)\frac{\partial v_{1z}}{\partial z}-\frac{R}{M}\frac{\partial T}{\partial z}$$
(8c)

Integration of the left and time sides of Eqs. (8a)-(8c) on time leads to the following results

$$\upsilon_{2r} = v \int_{0}^{t} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \upsilon_{1r}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2} \upsilon_{1r}}{\partial \varphi^{2}} + \frac{\partial^{2} \upsilon_{1r}}{\partial z^{2}} \right] d\tau - \int_{0}^{t} \left(\alpha_{2r} + \upsilon_{1r} \right) \frac{\partial \upsilon_{1r}}{\partial r} d\tau - \frac{1}{r} \int_{0}^{t} \left(\alpha_{2\varphi} + \upsilon_{1\varphi} \right) \frac{\partial \upsilon_{1\varphi}}{\partial \varphi} d\tau - \int_{0}^{t} \left(\alpha_{2z} + \upsilon_{1z} \right) \frac{\partial \upsilon_{1z}}{\partial z} d\tau - \frac{R}{M} \int_{0}^{t} \frac{\partial T}{\partial r} d\tau$$
(8d)

$$\upsilon_{2r} = v \int_{0}^{t} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \upsilon_{1\varphi}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2}\upsilon_{1\varphi}}{\partial \varphi^{2}} + \frac{\partial^{2}\upsilon_{1\varphi}}{\partial z^{2}} \right] d\tau - \int_{0}^{t} (\alpha_{2r} + v_{1r}) \frac{\partial \upsilon_{1r}}{\partial r} d\tau - \frac{1}{r} \int_{0}^{t} (\alpha_{2\varphi} + v_{1\varphi}) \frac{\partial \upsilon_{1\varphi}}{\partial \varphi} d\tau - \int_{0}^{t} (\alpha_{2z} + v_{1z}) \frac{\partial \upsilon_{1z}}{\partial z} \frac{\partial \upsilon_{1r}}{\partial r} d\tau - \frac{R}{rM} \int_{0}^{t} \frac{\partial T}{\partial \varphi} d\tau \\
\upsilon_{2z} = v \int_{0}^{t} \left[\frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial \upsilon_{1z}}{\partial r} \right) + \frac{1}{r^{2}} \frac{\partial^{2}\upsilon_{1z}}{\partial \varphi^{2}} + \frac{\partial^{2}\upsilon_{1z}}{\partial z^{2}} \right] d\tau - \int_{0}^{t} (\alpha_{2r} + v_{1r}) \frac{\partial \upsilon_{1r}}{\partial r} d\tau - \frac{1}{r} \int_{0}^{t} (\alpha_{2\varphi} + v_{1\varphi}) \frac{\partial \upsilon_{1\varphi}}{\partial \varphi} d\tau - \int_{0}^{t} (\alpha_{2z} + v_{1z}) \frac{\partial \upsilon_{1z}}{\partial z} d\tau - \frac{R}{M} \int_{0}^{t} \frac{\partial T}{\partial z} d\tau$$
(8f)

We determine the average values $\alpha 2r$, $\alpha 2\phi$, $\alpha 2z$ by the standard relations

$$\alpha_{2r} = \frac{1}{\pi \Theta R^2 L} \int_{0}^{\Theta R} \int_{0}^{R} \int_{-L}^{2\pi} \left(\nu_{2r} - \nu_{1r} \right) dz d\varphi dr dt,$$

$$\alpha_{2\varphi} = \frac{1}{\pi \Theta R^2 L} \int_{0}^{\Theta R} \int_{0}^{R} \int_{-L}^{2\pi} \left(v_{2\varphi} - v_{1\varphi} \right) dz d\varphi dr dt,$$

$$\alpha_{2z} = \frac{1}{\pi \Theta R^2 L} \int_{0}^{\Theta} \int_{0}^{R} r \int_{0}^{2\pi} \int_{0}^{L} (\upsilon_{2z} - \upsilon_{1z}) dz d\varphi dr dt \qquad (9)$$

Here Θ is the continuance of flowing of mixture of gases. Substitution of the approximations with the first- and the second-orders into the relation (9) gives the possibility to obtain system of equations for the considered average values

$$\begin{cases}
A_{1}\alpha_{2r} + B_{1}\alpha_{2\varphi} + C_{1}\alpha_{2z} = D_{1} \\
A_{2}\alpha_{2r} + B_{2}\alpha_{2\varphi} + C_{2}\alpha_{2z} = D_{2} \\
A_{3}\alpha_{2r} + B_{3}\alpha_{2\varphi} + C_{3}\alpha_{2z} = D_{3}
\end{cases}$$
(10)

Here
$$A_1 = 1 + \int_0^{\Theta} (\Theta - t) \int_0^R \int_0^{2\pi} \int_{-L}^L \frac{\partial v_{1r}}{\partial r} dz d\varphi dr dt$$
,
$$B_1 = \int_0^{\Theta} (\Theta - t) \int_0^{R} \int_{-L}^{2\pi} \int_{-L}^L \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr dt$$

$$C_1 = C_2 = \frac{\pi}{2} \Theta^2 R^2 V_2$$

$$\begin{split} &C_{1}=C_{2}=\frac{\pi}{2}\Theta^{2}R^{2}V_{0}\\ &D_{1}=v\int\limits_{0}^{\Theta R}\int\limits_{0}^{2\pi}\int\limits_{-L}^{L}\left[\frac{1}{r}\frac{\partial}{\partial r}\left(r\frac{\partial v_{1r}}{\partial r}\right)+\frac{1}{r^{2}}\frac{\partial^{2}v_{1r}}{\partial \varphi^{2}}+\frac{\partial^{2}v_{1r}}{\partial z^{2}}\right]dzd\varphi dr\left(\Theta-\frac{\partial v_{1r}}{\partial r}\right) \end{split}$$

$$-t\big)dt - \frac{\pi}{8}\Theta^2R^2V_0^2 - \int\limits_0^\Theta (\Theta - t) \int\limits_0^R \int\limits_0^{2\pi} \int\limits_{-L}^L v_{1r} \frac{\partial v_{1r}}{\partial r} dz d\varphi dr dt - \int\limits_0^\Theta \int\limits_0^{R2\pi} \int\limits_{-L}^L v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr \times V_0 + \int\limits_0^\Theta \int\limits_0^{R2\pi} \int\limits_{-L}^L v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr \times V_0 + \int\limits_0^\Theta \int\limits_0^{R2\pi} \int\limits_{-L}^L v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr \times V_0 + \int\limits_0^\Theta \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R \int\limits_{-L}^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dz d\varphi dr + \int\limits_0^\Theta \int\limits_0^R \int\limits_0^R v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dz dz d\varphi dz d\varphi dz d\varphi dz d\varphi dz d\varphi dz d\varphi dz d\varphi$$

$$(\Theta - t)dt,$$

$$A_2 = \int_0^{\Theta} (\Theta - t) \int_0^R r \int_{0-L}^{2\pi} \int_{0-L}^L \frac{\partial v_{1r}}{\partial r} dz d\varphi dr dt,$$

$$\begin{split} B_2 &= 1 + \int_{0}^{\Theta R} \int_{0}^{2\pi} \int_{-L}^{L} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr (\Theta - t) dt \end{split}$$

$$\times \int_{0}^{R} \int_{0-L}^{2\pi L} \int_{1}^{L} v_{1r} \frac{\partial v_{1r}}{\partial r} dz d\varphi dr dt - \int_{0}^{\Theta} (\Theta - t) \int_{0}^{R} \int_{0-L}^{2\pi L} v_{1\varphi} \frac{\partial v_{1r}}{\partial \varphi} dz d\varphi dr dt - \frac{\pi}{8} \Theta^{2} R^{2} V_{0}^{2}$$

$$C3 = 1 + \frac{\pi}{2} \Theta^{2} R^{2} V_{0}$$

$$B_{3} = \int_{0}^{\Theta} (\Theta - t) \int_{0}^{R} r \int_{0-L}^{2\pi} \frac{\partial v_{1z}}{\partial \varphi} dz d\varphi dr dt$$

$$-t \int \int _0^R r \int _0^{2\pi} \int _{-L}^L v_{1r} \frac{\partial v_{1z}}{\partial r} dz d\varphi dr dt - \int _0^\Theta \left(\Theta - t \right) \int _0^R r \int _{0-L}^{2\pi} \int _{1\phi}^L v_{1\phi} \frac{\partial v_{1z}}{\partial \varphi} dz d\varphi dr dt$$

Solution of the system of Eqs.(10) could be determine by standard approaches [12] and could be written as



$$\alpha_{2r} = \Delta_r / \Delta, \alpha_{2\varphi} = \Delta_{\varphi} / \Delta, \alpha_{2z} = \Delta_z / \Delta$$
(11)
where
$$\Delta = A_1 (B_2 C_3 - B_3 C_2) - B_1 (A_2 C_3 - A_3 C_2) + C_1 (A_2 B_3 - A_3 B_2)$$

$$-B_1 (D_2 C_3 - D_3 C_2) + C_1 (D_2 B_3 - D_3 B_2),$$

$$\Delta_{\varphi} = D_1 (B_2 C_3 - B_3 C_2) - B_1 (D_2 C_3 - D_3 C_2) + C_1 \times C_1$$

In this section we obtain the second-order approximations of components of speed of flow framework the method of averaging of function corrections. The second-order approximations is usually enough good approximations for qualitative analysis of the obtained solutions and to make several quantitative results.

 $\Delta_z = A_1(B_2D_3 - B_3D_2) - B_1(A_2D_3 - A_3D_2) + D_1(A_2B_3 - A_3B_2)$

 $\times (D_2B_2-D_2B_2)$

Eqs.(1) and (3) with using cylindrical coordinates could be written as

$$c\frac{\partial T}{\partial t} = \lambda \frac{\partial^2 T}{\partial r^2} + \lambda \frac{1}{r^2} \frac{\partial^2 T}{\partial \varphi^2} + \lambda \frac{\partial^2 T}{\partial z^2} + p - c \frac{\partial}{\partial r} (v_r CT) - \frac{c}{r} \frac{\partial}{\partial \varphi} (v_\varphi CT) - c \frac{\partial}{\partial z} (v_z CT)$$

(12

$$\frac{\partial C}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} \left(r D \frac{\partial C}{\partial r} \right) - \frac{1}{r} \frac{\partial}{\partial r} \left(r C \upsilon_r \right) + \frac{1}{r^2} \frac{\partial}{\partial \varphi} \left(D \frac{\partial C}{\partial \varphi} \right) - \frac{1}{r} \frac{\partial}{\partial \varphi} \left(C \upsilon_\varphi \right) + \frac{\partial}{\partial z} \left(D \frac{\partial C}{\partial z} \right) - \frac{\partial}{\partial z} \left(C \upsilon_z \right) \tag{13}$$

To calculate spatio-temporal distributions of temperature and concentration of growth component in gas mixture we also used method of averaging of function corrections. We determine the first-order approximations by their not yet known average values $\alpha 1T$ and $\alpha 1C$ in right sides of the above equations. Using recently considered algorithm gives us possibility to obtain relations for the first-order approximations of the considered temperature and concentration in the following form

$$T_{1}(r,\varphi,z,t) = T_{r} + \int_{0}^{t} \frac{p(r,\varphi,z,\tau)}{c} d\tau - \alpha_{1T}\alpha_{1C} \int_{0}^{t} \frac{\partial v_{r}(r,\varphi,z,\tau)}{\partial r} d\tau - \frac{\alpha_{1T}\alpha_{1C}}{r} \int_{0}^{t} \frac{\partial v_{\varphi}(r,\varphi,z,\tau)}{\partial \varphi} d\tau - \alpha_{1T}\alpha_{1C} \int_{0}^{t} \frac{\partial v_{z}(r,\varphi,z,\tau)}{\partial z} d\tau$$

$$(14)$$

$$C_{1}(r,\varphi,z,t) = -\alpha_{1T}\alpha_{1C}\int_{0}^{t} \frac{\partial v_{r}(r,\varphi,z,\tau)}{\partial r} d\tau - \frac{\alpha_{1C}}{r}\int_{0}^{t} \frac{\partial [rv_{r}(r,\varphi,z,\tau)]}{\partial r} d\tau - \frac{\alpha_{1C}}{r}\int_{0}^{t} \frac{\partial [rv_{r}(r,\varphi,z,\tau)]}{\partial r} d\tau$$

$$-\frac{\alpha_{1C}}{r} \int_{0}^{t} \frac{\partial v_{\varphi}(r,\varphi,z,\tau)}{\partial \varphi} d\tau - \alpha_{1C} \int_{0}^{t} \frac{\partial v_{z}(r,\varphi,z,\tau)}{\partial z} d\tau$$
(15)

We determine the average values $\alpha 1T$ and $\alpha 1C$ by using the standard relations

$$\alpha_{1T} = \frac{1}{\pi \Theta R^2 L} \int_{0}^{\Theta R} \int_{0}^{2\pi} \int_{-L}^{L} T_1(r, \varphi, z, \tau) dz d\varphi dr dt$$

$$\alpha_{1C} = \frac{1}{\pi \Theta R^2 L} \int_{0}^{\Theta R} \int_{0}^{R} r \int_{0}^{2\pi} \int_{-L}^{L} C_1(r, \varphi, z, \tau) dz d\varphi dr dt$$
(16)

Substitution of the calculated the first-order approximations into the relations (16) gives a possibility to obtain the following result [12]

$$\alpha_{1C} = C_0 / L \cdot \left[1 + \frac{1}{\pi \Theta R L} \int_0^{\Theta} (\Theta - t) \int_0^{2\pi} \int_{-L}^{L} v_r(R, \varphi, z, t) dz d\varphi dt + \frac{\Theta V_0}{R L} \right]$$

$$\alpha_{1T} = \left[T_r + \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R \int_0^{2\pi} \int_{-L}^L \frac{p(r, \varphi, z, t)}{c} dz d\varphi dr dt \right] \left\{ 1 + \frac{C_0}{\pi \Theta R L^2} \left[\int_0^{\Theta} (\Theta - t) \times \frac{1}{2\pi \Theta R L^2} \right] \right\}$$

$$\times \int_{0}^{2\pi} \int_{-L}^{L} v_r(R,\varphi,z,\tau) dz d\varphi dt - \frac{1}{\pi \Theta R^2} \int_{0}^{\Theta} (\Theta - t) \int_{0}^{R2\pi} \int_{0}^{L} v_r(r,\varphi,z,\tau) dz d\varphi dr dt + \frac{V_0}{2} \bigg] \times$$

$$\times \left[1 + \frac{1}{\pi \Theta R L} \int_{0}^{\Theta} (\Theta - t) \int_{0}^{2\pi} \int_{-L}^{L} v_{r}(R, \varphi, z, t) dz d\varphi dt + \frac{\Theta V_{0}}{R L} \right]^{-1} \right\}$$

$$(17)$$

The second-order approximations of the temperature and the concentrations have been calculated framework standard procedure of method of averaging of function correction [7-11]. Framework the approach we replace the required functions in right sides of Eqs. (12) and (13) on the following sums: $T \rightarrow \alpha_{2T} + T_1$, $C \rightarrow \alpha_{2C} + C_1$. In this situation the second-order approximations could be written as

$$\begin{split} &c\cdot T_{2}(r,\varphi,z,t) = \lambda_{0}^{i}\frac{\partial^{2}T_{1}(r,\varphi,z,\tau)}{\partial r^{2}}d\tau + \lambda\frac{1}{r^{2}}\frac{\partial^{2}T_{1}(r,\varphi,z,\tau)}{\partial \varphi^{2}}d\tau + \lambda_{0}^{i}\frac{\partial^{2}T_{1}(r,\varphi,z,\tau)}{\partial z^{2}}d\tau + \\ &+ \int_{0}^{t}p(r,\varphi,z,\tau)d\tau - c\cdot\frac{\partial}{\partial r}\int_{0}^{t}\left\{v_{r}(r,\varphi,z,\tau)\cdot\left[\alpha_{2C} + C_{1}(r,\varphi,z,\tau)\right]\cdot\left[\alpha_{2T} + T_{1}(r,\varphi,z,\tau)\right]\right\}d\tau + \\ &+ T_{r} - \frac{c}{r}\frac{\partial}{\partial \varphi}\int_{0}^{t}\left\{v_{\varphi}(r,\varphi,z,\tau)\cdot\left[\alpha_{2C} + C_{1}(r,\varphi,z,\tau)\right]\cdot\left[\alpha_{2T} + T_{1}(r,\varphi,z,\tau)\right]\right\}d\tau - \end{split}$$

$$-c \cdot \frac{\partial}{\partial z} \int_{0}^{t} \left\{ v_{r}(r, \varphi, z, \tau) \cdot \left[\alpha_{2C} + C_{1}(r, \varphi, z, \tau) \right] \cdot \left[\alpha_{2T} + T_{1}(r, \varphi, z, \tau) \right] \right\} d\tau$$
(18)



$$C_{2}(r,\varphi,z,t) = \frac{1}{r} \frac{\partial}{\partial r} \left[r D \frac{\partial C_{1}(r,\varphi,z,\tau)}{\partial r} d\tau + \frac{1}{r^{2}} \frac{\partial}{\partial \varphi} \left[D \frac{\partial C_{1}(r,\varphi,z,\tau)}{\partial \varphi} d\tau + \frac{\partial}{\partial z} \left[D \times \frac{\partial C_{1}(r,\varphi,z,\tau)}{\partial \varphi} d\tau - \frac{1}{r} \frac{\partial}{\partial z} \left[\alpha_{2C} + C_{1}(r,\varphi,z,\tau) \right] \cdot v_{r}(r,\varphi,z,\tau) d\tau \right] \right] - \frac{1}{r} \frac{\partial}{\partial \varphi} \left[v_{\varphi}(r,\varphi,z,\tau) \cdot \left[\alpha_{2C} + C_{1}(r,\varphi,z,\tau) \right] \cdot v_{z}(r,\varphi,z,\tau) d\tau \right] + C_{0} \delta(z+L)$$

$$(19)$$

Average values of the second-orders of the considered temperature and concentration $\alpha 2T$ and $\alpha 2C$ have been determined by the following standard relations

$$\alpha_{2T} = \frac{1}{\pi \Theta R^{2} L} \int_{0.0}^{\Theta R} \int_{0.-L}^{T} (T_{2} - T_{1}) dz d\varphi dr dt$$

$$\alpha_{2C} = \frac{1}{\pi \Theta R^{2} L} \int_{0.0}^{\Theta R} r \int_{0.-L}^{2\pi L} (C_{2} - C_{1}) dz d\varphi dr dt$$
(20)

Substitution of the first- and the second-orders of temperature and concentration into the relations (20) gives us possibility to obtain relations for the appropriate average values in the following form

$$\alpha_{2T} = \left(\frac{\lambda \sigma}{c \pi \Theta R L} \int_{0}^{\Theta} (\Theta - t) \int_{0}^{2\pi} \int_{-L}^{L} T^{4}(R, \varphi, z, t) dz d\varphi dt - \int_{0}^{\Theta} (\Theta - t) \int_{0}^{2\pi} \int_{-L}^{L} T_{1}(R, \varphi, z, t) dz d\varphi dt \times \right)$$

$$\times \left[\left[\alpha_{2c} + C_1(R, \varphi, z, t) \right] T_1(R, \varphi, z, t) - \alpha_{1T} \alpha_{1c} \right\} dz d\varphi dt \frac{1}{\pi \Theta R L} - \frac{1}{\pi \Theta R^2 L} \int_0^{\varphi} \left(\Theta - t \right) \times dz d\varphi dt dt$$

$$\times \int\limits_{0}^{R^{2\pi}} \int\limits_{0}^{L} v_{r}(r,\varphi,z,\tau) \{T_{1}(r,\varphi,z,t)[\alpha_{2C}+C_{1}(r,\varphi,z,t)] - \alpha_{1T}\alpha_{1C}\} dz d\varphi r dr dt - \frac{V_{0}}{\pi \Theta R^{2}L} \times \frac{V_{0}}{R^{2}} + \frac{V_{0}}{R^{2}}$$

$$\times \int\limits_{0}^{\Theta} \left(\Theta - t\right) \int\limits_{0}^{R} r \int\limits_{0}^{2\pi} \left[\left(\alpha_{2C} + C_{0}\right) \cdot T_{1}\left(r, \varphi, L, t\right) - \alpha_{1T}\alpha_{1C}\right] d\varphi dr dt \left\{ 1 + \frac{1}{\pi \Theta RL} \int\limits_{0}^{\Theta 2\pi} \int\limits_{0}^{L} V_{r}\left(R, \varphi, z, t\right) \times \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2}$$

$$\times \left[\alpha_{2C} + C_1(R, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] \times \frac{1}{2\pi \Omega L} \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dt - \frac{1}{\pi \Theta R^2 L} \int_0^{\Theta} (\Theta - t) \int_0^R r \int_0^{2\pi} \int_{-L}^L \left[\alpha_{2C} + C_1(r, \varphi, z, t)\right] dz d\varphi(\Theta - t) dz d\varphi(\Theta - t)$$

$$\times v_{r}(r,\varphi,z,\tau) dz d\varphi dr dt + 2V_{0}(\alpha_{2C} + C_{0}) \frac{\Theta}{L}$$

$$\alpha_{2C} = \frac{1}{\pi \Theta R^{2}L} \int_{0}^{\Theta} (\Theta - t) \int_{0}^{R} r \int_{0}^{2\pi} D \left[\frac{\partial C_{1}(r,\varphi,z,\tau)}{\partial z} \Big|_{z=L} - \frac{\partial C_{1}(r,\varphi,z,\tau)}{\partial z} \Big|_{z=L} \right] d\varphi dr dt - \frac{1}{\pi \Theta R^{2}L} \int_{0}^{\Theta} (\Theta - t) \int_{0}^{2\pi} \int_{0}^{L} \{r[\alpha_{2C} - \alpha_{1C} + C_{1}(R,\varphi,z,\tau)] \cdot v_{r}(R,\varphi,z,\tau)\} dz d\varphi dt$$

$$-\frac{V_0}{\pi\Theta R^2L}\int\limits_0^\Theta \left(\Theta-t\right)\int\limits_0^R r\int\limits_0^{2\pi} \left(\alpha_{2C}-\alpha_{1C}+C_0\right)dzd\varphi drdt$$

3 Discussion

In this section we used relations (8,9,18-20) analyzed spatio-temporal distributions of temperature and concentration of growth component in flow of gas mixture on frequency of rotation of disk keeper of substrate ω and diffusion coefficient during MOCVD epitaxy of gallium arsenide (see Figs. 2 and 3). The considered results have been obtained for the following case: gas-carrier hydrogen, internal diameter of reaction chamber d =200 mm, diameter of disk keeper of substrate is d1 = 160 mm, volumetric speed of flow is 10 liter/min; frequency of rotating of keeper of substrate is ω = 20 rad/min; specific length of reaction chamber is L =200 mm.

Fig. 2a shows monotonous increasing of the considered stationary concentration C at constant value of concentration C0 in inlet area of reaction chamber. In this situation one can obtain increasing of speed of epitaxial growth with increasing frequency of rotation ω . The Fig. 2b shows dependence of the considered stationary concentration on value of

diffusion coefficient D. The figure shows, that increasing of diffusion

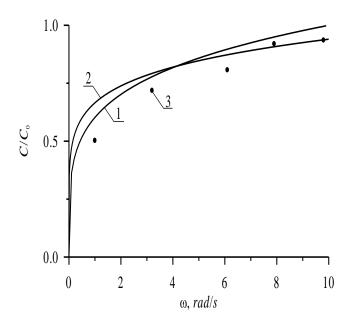


Fig 2a. Dependences of stationary concentration of growth component C in center of disk keeper of substrate on frequency of rotating ω at constant value of concentration C0 in inlet area of reaction chamber. Solid lines are calculated dependences.

Points are experimental results. Curve 1 corresponds to atmospheric pressure. Curve 2 corresponds to low pressure (0.1 of atmospheric pressure)

coefficient leads to increasing of speed of transport of growth component. In this situation one can find decreasing of concentration of growth component in area of growth. Curves 1 on Figs. 2 correspond to atmospheric pressure in reaction chamber. Curves 1 on Figs. 2 correspond to low pressure (0.1 of atmospheric pressure) inreaction chamber. Dependence of concentration of mixture of gas on kinematics viscosity ν is enough weak for the considered conditions of epitaxy process. In this situation we do not consider the dependence.

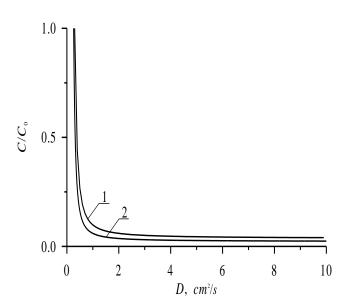


Fig 2b. Dependences of stationary concentration of growth component C in center of disk keeper of substrate on diffusion coefficient D at constant value of concentration C0 in inlet area of reaction chamber. Curve 1 corresponds to atmospheric pressure. Curve 2 corresponds to low pressure (0.1 of atmospheric pressure).

All considered dependences (Fig. 2) show faster changing of concentration with faster changing of concentration with faster achievement of saturation with low temperature in comparison with growth of epitaxial layer at atmospheric pressure. The Fig. 2a is also shows comparison of theoretical results (solid lines) with experimental one (points) for MOCVD epitaxy of gallium arsenide at low pressure. Using experimentally measured values (speed of growth of epitaxial layer and frequency of rotation of keeper of substrate) and accounting linear dependence of speed of growth on concentration of main growth component of growth component of gas mixture CO

trimethylgallium [2,5] we obtain experimental dependence C/C0 on ω (Fig. 2a). We find enough good coincidence of experimental dependence with experimental one. Reason of some mismatch of experimental and theoretical data is probably side reaction in gas phase [5]. Framework the reaction a part of gallium arsenide do not transit in a solid phase in reaction zone. Similar experimental dependence of C/C0 on ω has been also obtained in [11].

Analysis of distribution of temperature near disk keeper of substrate shows more homogenous spatial distribution of the temperature in the middle of the keeper and decreasing of the temperature on the edges of the keeper because of heat losing due to convective heat exchange. Dependence of temperature in gas phase on radial coordinate r is illustrated by Fig. 3a. We also show dependence of temperature in gas phase on axial coordinate z (see Fig. 3b). The Figs. 3 show stationary distribution of temperature. Characteristics of temperature define development of reactions of individual thermal decomposition of main components and dopants of flow of mixture of gases during epitaxy of semiconductor layers.

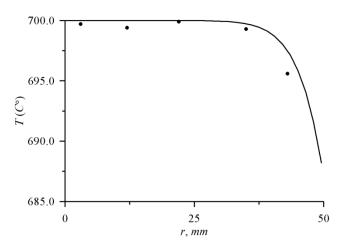


Fig 3a. Dependences of stationary temperature in keeper of substrate on radial coordinate z. Points are experimental data.



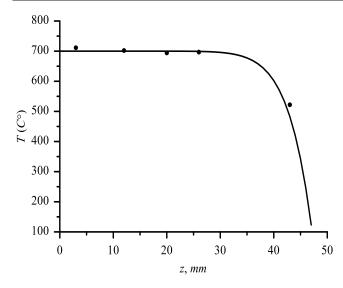


Fig. 3b. Dependences of stationary temperature in keeper of substrate on axial coordinate z. Points are experimental data.

4 Conclusions

In this paper we introduce an analytical approach to model of physical processes, which could be find during epitaxy from gas phase, with account rotating disk keeper of substrate. We estimate spatio-temporal distributions of concentration of growth component and temperature in flow of mixture of gases. Analysis of influence of technological parameters on the above distributions have been done. We illustrate good agreement between our calculated results and experimental one. In this situation our model is enough adequate.

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References

- Molecular-beam epitaxy and heterostructures edited L. Cheng, K. Plog, "Mir", Moscow (1989).
- [2] M.A. Herman, W. Richter, H. Sitter. Epitaxy Physical Principles and Technical Implementation, Springer, Berlin (2004).
- [3] G.B. Stringfellow. Organometallic Vapor-phase Epitaxy: Theory and Practice. Academic Press, Boston (1989).
- [4] R.A. Talalaev, E.V. Yakovleva, S.Yu. Karpova, Yu.N. Makarov. J. Cryst. Growth. Vol. 230. P. 232-238 (2001).
- [5] W.V. Lundin, A.V. Sakharov, E.E. Zavarin, M.A. Sinitsyn, A.E. Nikolaev, G.A. Mikhailovsky, P.N. Brunkov, V.V.

- Goncharov, B.Ya. Ber, D.Yu Kazantsev, A.F. Tsatsul'nikov. Semoconductors. Vol. 43 (7). P. 996-1001 (2009).
- [6] H.S. Carslaw, J.C. Jaeger. Conduction of heat in solids. Oxford: At the Clarendon Press. 1964. 488 p.
- [7] Yu.D. Sokolov. Applied Mechanics. Vol.1 (1). P. 23-35 (1955).
- [8] E.L. Pankratov. J. Comp. Theor. Nanoscience. Vol. 9 (1). P. 41-49 (2012).
- [9] E.L. Pankratov, E.A. Bulaeva. International Journal of Micro-Nano Scale Transport. Vol. 3 (3). P. 119-130 (2012).
- [10] E.L. Pankratov, E.A. Bulaeva. Reviews in Theoretical Science. Vol. 1 (1). P. 58-82 (2013).
- [11] E.L. Pankratov, E.A. Bulaeva. Reviews in Theoretical Science. Vol. 3 (4). P. 365-398 (2015).
- [12] G. Korn, T. Korn. Mathematical Handbook for scientists and engineers. Definitions, theorems and formulas for reference and review. Second edition. McGraw-Hill Book Company. New York, 1968.